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# INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS

ANOMALOUS LEPTON-HADRON INTERACTIONS AND GAUGE MODELS

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and

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INTERNATIONAL ATOMIC ENERGY AGENCY



UNITED NATIONS EDUCATIONAL, SCIENTIFIC AND CULTURAL ORGANIZATION

**1974 MIRAMARE-TRIESTE** 

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18 November 1974

IC/74/81 ADDENDUM

ANOMALOUS LEPTON-HADRON INTERACTIONS AND GAUGE MODELS

Jogesh C. Pati and Abdus Salam

#### ADDENDUM

It is possible to avoid  $K \rightarrow \mu e$ -decays without putting the electron and the muon in different fermionic multiplets, if we introduce an extended gauge group as follows.

Assume that the gauge group is  $SU(16)_L \ge SU(16)_R$ , so that the 16-fold of  $F_L$  and the 16-fold of  $F_R$  in the basic model (see Eq. (A.1)) transform as (16, 1) and (1, 16) respectively under this gauge group. (Such a gauge group would in any case be desirable from the point of view of complete unification of all forces and would involve only one basic coupling constant assuming that the theory possesses left  $\leftrightarrow$  right-discrete symmetry in the gauge sector.) Clearly, this extended group can contain the gauge group  $SU(2)_L \ge SU(2)_R$  $\ge SU(3^4)_{L+R}$  of the basic gauge model. The important new feature, however, is that spontaneous symmetry breaking may allow the four sets of X-perticles carrying different valencies (in this case) to remain <u>unmixed</u> and <u>chiral</u> with their couplings given by

$$f\{(x_{p}^{\circ})_{L}(\tilde{v}_{P_{a}})_{L} + (x_{n}^{\circ})_{L}(\bar{c}n_{z})_{L} + (x_{\lambda}^{\circ})_{L}(\bar{\mu}\lambda_{a})_{L} + (x_{\lambda}^{\circ})_{L}(\tilde{v}^{\dagger}\chi_{a})_{L}\}$$

$$+ f\{(x_{p}^{\circ})_{L}(\tilde{v}_{P_{b}})_{L} + (x_{n}^{\circ})_{L}(\bar{c}n_{b})_{L} + (x_{\lambda}^{\circ})_{L}(\bar{\mu}\lambda_{b})_{L} + (x_{\lambda}^{\circ})_{L}(\tilde{v}^{\dagger}\chi_{b})_{L}\}$$

$$+ f\{(x_{p}^{\circ})_{L}(\bar{v}_{P_{c}})_{L} + (x_{n}^{\circ})_{L}(\bar{c}n_{c})_{L} + (x_{\lambda}^{\circ})_{L}(\bar{\mu}\lambda_{c})_{L} + (x_{\lambda}^{\circ})_{L}(\tilde{v}^{\dagger}\chi_{c})_{L}\}$$

$$+ (L + R) + h.c.$$

where we assume that  $X_p \neq X_n \neq X_\lambda \neq X_\chi$  and the masses of all these particles are different. (Note that the valency quantum numbers (p, n,  $\lambda$ ,  $\chi$ ) of the fermions and, therefore, of the currents are fixed essentially by the "observed" weak-interactions. In writing the above we have set the electron to be "non-strange" with its neutrino  $\nu$  "uncharmed" and the muon to be "strange" with its neutrino  $\nu$ " "charmed", although <u>a priori the opposite choice is</u> <u>equally permissible</u>. Note that Eq. (A.5) would reduce to Eq. (A.2) if we set  $X_p = X_p = X_\lambda = X_\lambda$ ]

With  $X_n \neq X_{\lambda}$  (unlike the basic gauge model), the X-interactions may no longer induce  $K \Rightarrow \overline{\mu}e$ -decays. They do not, of course, induce  $K \Rightarrow \overline{e}e$  or  $K \Rightarrow \overline{\mu}\mu$ decays, if we assume that both sets of  $(\lambda, n)$  and  $(\mu, e)$  are Cabibbo-rotated with the same angle. (This is analogous to  $(\lambda, n)$  and  $(e, E^-)$  being Cabibborotated in the same manner in the prodigal model.)

Furthermore, with  $X_p \neq X_n$  and  $X_p \neq X_\lambda$ , the X-interactions cannot induce  $\beta$ -decays  $(n \rightarrow p+e^- + \bar{\nu}_e)$  and  $K^+ \rightarrow \mu^+ + \nu_e$ -decays. This again is in contrast to the basic gauge-model.

The major restriction on the strength of  $Y_p$ -interactions arises from considerations of the semi-leptonic "neutral-current"-processes (involving "uncharmed" neutrinos), i.e.  $v + N \Rightarrow v + H$ , etc. Now, if the spontaneous symmetry-breaking mechanism (which must preserve SU(3')<sub>L+R</sub> as a good symmetry) at the same time forces the masses of the X-particles to be approximately equal, i.e.  $M_{\chi_p} \cong M_{\chi_n} \cong M_{\chi_\lambda} \cong H_{\chi_\chi}$ , then the fact that the observed strength of these "neutral-current"-neutrino-interactions is of order  $G_{permi}$ would imply that the X-mechanism will not be relevant for the observed enhancement of electron-hadron-interactions at SPEAR energies. We have not yet investigated by an actual construction of the symmetry-breaking terms if this is indeed the case. But even if it is, there still remains one interesting exception, which we mention below.

Assume that the  $X_L$ 's and the  $X_R$ 's, which are coupled to left-and righthanded currents respectively, are eigen states of the mass matrix (rather than their linear combinations) and that it is the  $X_R$ 's, which are light and relevant for the enhanced electron-hadron-interaction with

## $M_{\chi_L} >> M_{\chi_R}$

In this case, one should expect enhanced "diagonal"-interactions of only the right-handed neutrinos and left-handed anti-neutrinos with hadrons; but the interactions of hadrons with left-handed neutrinos and right-handed antineutrinos (which the basic model contains and which on account of the assumed chirality<sup>41</sup> of the interactions in the present case can also be massless) would still be suppressed. As far as one knows, experimentally, it is at least permissible to assume that the available neutrino-beams in the laboratory consist predominantly of neutrinos of the latter variety (i.e.  $v_1$ 'S and  $\bar{v}_p$ 'S). Thus the observed strength of order  $G_{\rm Fermi}$  for reactions of the variety  $v + N \rightarrow v + H$ ) (where the neutrinos are predominantly  $v_{\nu}^{*}S$  and  $\bar{v}_{\nu}^{*}S$ ) does not exclude the possibility that the effective strength of the  $X_p$ mediated interactions is of order  $(\alpha/50)(\text{BeV})^{-2}$ . One may therefore attribute the CEA-SPEAR enhancement to the interactions mediated by these X<sub>p</sub>-particles, which are coupled to the <u>right-handed</u> currents. If this explanation is to apply, one would predict (i) large parity violation in  $e^{-}e^{+} \rightarrow$  hadrons and other related processes at SPEAR-energies (and similarly for the muon-induced reactions) and (11) enhanced interactions of neutrinos of the unfamiliar helicities (i.e.  $\nu_{h}^{*}S$  and  $\bar{\nu}_{L}^{*}S)$  with hadrons at presently available energies (even though neutrinos of the familiar helicities (i.e.  $v_t^T S$  and  $\bar{v}_p^T S$  ) may interact with a strength of order G<sub>Fermi</sub>). This would manifest itself in enhanced rates for decays of the type  $\eta \Rightarrow \pi^0 + \nu_R + \bar{\nu}_L$ . [Note that the neutrinos in question must be "uncharmed" (i.e. those which couple to the protonquarks via X. These way be either  $v_{1}^{*}S$  or  $v_{1}^{*}S$  depending on the details of the model. Rough estimates with  $\frac{f^2}{m_{X_D} z} \approx 10^{-3}$  indicate that  $\frac{\Gamma(\eta \Rightarrow \pi^0 \pm \upsilon_R \pm \upsilon_L)}{\Gamma(\eta \Rightarrow \pi^0 \pm \gamma \pm \gamma)}$ may be of order 1-10%, which is about four orders of magnitude higher than what would be given by an effective interaction strength of  $G_{permid}$ .

In summary, the chiral nature of the colour-gauge interactions and the assumption of the distinctions of  $X_p$ ,  $X_n$ ,  $X_\lambda$  and  $X_{-\chi}$  from each other (something, which is permissible within the extended gauge structure, but not in the basic gauge-model) leads to a number of new experimental possibilities including

-3-

the lowering of the energy at which the anomalous electron-hadron interactions mediated via the X-particles become effective. Thus in <u>contrast</u> to the prodigal-model:

 Both the electron and the muon may exhibit anomalous interactions with hadrons at present energies with <u>either</u> one of them being "strenge" and the other "non-strange".

(2) With the condition  $M_{X_{L}} > M_{X_{p}}$ , which provides one likely solution <sup>48</sup> for the model to be relevant to SPEAR results in the first place, one should expect to see large parity-violation in  $e^{-e^+}$  + hadrons and other related processes as well as <u>enhanced</u> interactions of the right-handed ("unfamiliar" helicity) neutrinos permitted by the basic model (either  $v_{e}$  or  $v_{\mu}$ ) with hadrons, even though the left-handed ("familiar helicity) neutrinos couple with an effective strength ~  $G_{\text{Fermi}}$ . The question of parity non-conservation may be tested by starting with polarised  $e^-$  and  $e^+$  beams and looking for possible  $\langle \vec{o} \rangle \cdot \vec{p}$ -type correlation (where  $\vec{p}$  is the momentum of a given outgoing hadron).

On the theoretical side, one needs to examine, with this extended gauge structure, whether an allowed pattern of spontaneous symmetry breaking  $^{49}$  with Higgs-Kibble multiplets would lead to the desired solutions; in particular, it must leave the X-particles of different valencies enmixed and must ensure the emergence of a global (or locel) SU(3') colour symmetry commuting with the familiar global SU(3)-symmetry. The model as it stands, possesses Adler-Bell-Jackiw anomalies, the resolution of which (as long as one assumes a gauge group of the type SU(n)<sub>L</sub> x SU(n)<sub>R</sub> with n  $\geq$  3 would have to involve the unattractive introduction of a new set of fermions F' (the two sets F and F' must then couple with opposite chiralities to the same set of gauge bosons and F' would have to be associated with new heavier quarks and leptons). Finally, the model contains a whole bost of new currents, which change both colour as well as valency quantum numbers. The corresponding gauge-mesons are presumably super-heavy and ineffective for the interactions considered in this paper in the low and intermediate energy range. Notwithstanding these theoretical problems, if blac experiments revent range party violating effects and also if both electron and muon exhibit anomalous interactions with hadrons at presently available energies, one will have to entertain this model very seriously.

#### FOOTNOTES TO ADDENDUM

48. A second interesting possibility within this extended gauge model is worth noting. It arises even if  $X_p$  is not lighter than  $\boldsymbol{X}_{_{\!\boldsymbol{T}}}$  and also even if X-interactions are parity conserving (so that  $(X_{L} + X_{R})\sqrt{2}$  are the eigenstates of the mass matrix). Noting that only the "uncharmed" neutrinos (which are coupled to the proton-quarks via X<sub>n</sub>) can exhibit their anomalous interactions with normal hadrons, if the electron-neutrinos are "uncharmed" (and therefore the muon-neutrinos are "charmed"), the X-interactions can induce reactions of the type  $v_{\mu} + N \xrightarrow{\Lambda_{p}} v_{\mu} + H$ , but not of the type  $v_{\mu} + N \xrightarrow{X} v_{\mu} + H$ . On the other hand, the <u>evailable</u> neutrino-beams contain primarily muon-neutrinos (with less than 2% contamination of electron-neutrinos). Thus the observed strength of order  $G_{permit}$  for the reactions v + N + v + H can still allow for the X-induced "diagonal"interactions of electron-neutrinos with hadrons to possess anomalous strength (as large as 5 to 10 times bigger than  $G_{\rm Fermi}$ ), even though much neutrinos may interact with hadrons with normal strength (order G<sub>Fermi</sub>). A test of this possibility with beams designed to contain a large fraction of electron-neutrinos would be worthwhile. For this possibility to be compatible with SPEAR-results, one must of course assume  $(f^2/m^2_{X_n})$  to at least an order of magnitude bigger than  $(f^2/m^2_{X_n})$ . Also worth noting is that if  $X_p$ -interactions are parity conserving (i.e.  $(x_{P_{L}} \pm x_{P_{L}})/\sqrt{2}$  are the eigenstates), the anomalous v<sub>e</sub>-interactions leading to  $v_p + N + v_p + H$  should possess, in general, large scalar, pseudo-scalar, vector and axial-vector interactions after Fiers-reshuffling (see Sec. II). The presence of scalar and pseudo-scalar terms may be desirable if the new Argonnedata on pion-production in "neutral current"-processes is sustained (see S. Adler, to be published). If the effect is confirmed, one may attribute it in this extended model primarily so vector or axial-vector-X-induced-neutrino interactions (either  $v_{e}$ 's or  $v_{t}$ 's). 49. This will be considered elsewhere in collaboration with Dr. R. N. Mohapatra.

-4-

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23 September 1974

IC/74/81 ADDENDUM

## ANOMALOUS LEPTON-HADRON INTERACTIONS AND GAUGE MODELS.

Jogesh C. Pati and Abdus Salam

### ADDENDUM

An explanation of  $e^+e^- \rightarrow$  hadrons starting from the weak interaction Lagrangian was given by P. Budini and P. Furlan (ICTP, Trieste, preprint IC/74/56). The most crucial prediction of this model is that the magnitude of the constant cross-section is derived without introducing new parameters from the hypothesis that the Yang-Mills gauge fields and the photon are composite objects generated dynamically by the weak Lagrangian.

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# International Atomic Energy Agency

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United Nations Educational Scientific and Cultural Organization

INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS

ANOMALOUS LEPTON-HADRON INTERACTIONS AND GAUGE MODELS \*

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MIRAMARE - TRIESTE August 1974

\* To be submitted for publication.

\*\* Supported in part by the National Science Foundation Grant No. GP 43662-X.

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#### ABSTRACT

Parameters for anomalous lepton-hadron interactions (like their signs, V and A-character and allowed and forbidden nature of certain transitions) are abstracted from the class of gauge models proposed earlier by the authors. This information is used to determine the strength of the anomalous interactions by fitting e e-annihilation data. We then make quantitative estimates of the energy-dependence of this cross-section, the deviation of the ratio of  $(e^{\dagger}p/e^{-}p)$  cross-sections from unity at high  $q^2$ , and (apparent) deviations from scaling in epscattering. Also discussed are consequences of anomalous interactions (with the restrictions mentioned above) on enhanced lepton-production in hadronic collisions, hyperfine structure splitting in hydrogen and leptonic decay modes of  $\pi^0$  and  $\eta$  . On the theoretical side, we discuss a variant of the basic gauge model (which allows the anomalous lepton-hadron interactions to be relevant at present energies). The major conclusion of this paper both from the theoretical side (taking into account restrictions on low-energy neutrino interactions) and from the phenomenological side (taking into account data on  $e^{\pm}$  alone) is that the electron is likely to be "strange", if its interaction with hadrons is "anomalous" at present energies. Further data is needed to test this possibility and also whether the muon is anomalous and strange or non-strange. It may of course be that leptons do possess anomalously strong interactions but only at high energies proposed in our basic gauge model, in which case such interactions are irrelevant for SLAC energies.

-1-

#### INTRODUCTION

In attempting to unify baryons and leptons within a guage theory context, we postulated in 1973 a new class of lepton-hadron interactions which eventually must acquire the same strength as hadron-hadron interactions. For the so-called basic model of leptons and hadrons, which was examined in detail in an earlier paper, there appeared theoretical limitations so that it was estimated that the new anomalous interaction would manifest itself for energies in the region of  $10^4$  BeV.

1)

Experimentally, however, the CEA-SPEAR enhancement  $3^{(3)}$   $e^+ + e^- \rightarrow$  hadrons might possibly be indicative of the fact that the mechanism suggested by us may already have become operative at much lower energies, and this suggestion was advanced in a letter.<sup>4)</sup> It was pointed out in this letter that

i) experimental studies involving energy dependence and the magnitude of  $\sigma(e^{-e^{+}} + hadrons)$ ,

ii) deviations of the ratios of  $(e^+p/e^-p)$  and  $(\mu^+p/\mu^-p)$  total cross-sections from unity at high  $q^2$ ,

iii) scaling behaviour of e + p + e + hadrons and apparant deviations therefrom, may provide further information on the existence and nature of such anomalous

interactions. In this paper we give quantitative estimates of the above effects and discuss other possible tests including enhancement of lepton production in hadron collisions.<sup>5)</sup> In making these estimates, we rely heavily on gauge models for obtaining the basic parameters of the anomalous interaction (like coupling strengths, their signs, (V and A)-character of these interactions and the allowed and forbidden nature of certain transtions). On the dynamical side we make use of the parton-model hypothesis in order to get a feeling for the magnitude of these effects. We are prompted to make such estimates by the fact that some of the experiments relevant for testing our ideas are in progress and some are already completed (in particular the ratio of  $e^{\dagger}p/e^{-}p$  total cross-section<sup>6)</sup> for  $q^{2}$  up to -15 (BeV)<sup>2</sup>, while similar data on  $\mu^{+}p/\mu^{-}p$  is expected <sup>7)</sup> to be available in the near future. Our chief conclusion is that the electron is likely to be a "strange" particle and its neutrino "charmed" in the sense of our gauge models, and this would imply an enhanced production of  $\phi^0$  and  $\eta^0$ 's and possibly also  $K\overline{K}$  as SLAC energy increases. In an appendix to the paper we discuss an explicit variant of our original model, to show that limitations on the relevant energies of the basic model can be relaxed, so that anomalous lepton-hadron interaction can begin to manifest itself with the requisite strength at the present low SLAC energies.

-2-

We, however, consider the new variant to be of a forced model and would hope that, if the electron does prove to be strange, a somewhat more attractive version of it emerges.

#### II. ANOMALOUS LEPTON-HADRON INTERACTIONS

The anomalous interactions of the charged leptons (e and 1) with quarks, which arise in the gauge theory context of Ref.2 and which are further discussed in Appx.I of this paper, are given by:

$$\mathcal{L}_{X} = f_{e}^{V}(\overline{e} \gamma_{\alpha} q_{e}) \chi_{e\alpha}^{V} + f_{e}^{A}(\overline{e} i\gamma_{\alpha}\gamma_{5} q_{e}) \chi_{e\alpha}^{A} + (e \neq \mu) + h.c. , \qquad (3)$$

where  $q_e$  denotes the specific quark (in our case it is <u>either</u> n <u>or</u>  $\lambda$ ) coupled to the electron via the X's; similarly for  $q_{\mu}$ . Since there is a triplet of X's corresponding to three baryonic colours, a summation over the colour-index of the quarks and of the X's is implied. In general the vector fields  $X_{e,\mu}^V$  may not be identical with the axial vector fields  $X_{e,\mu}^A$  and  $e_{\mu}$  parity is conserved. (One may, however, also consider the case  $X^V = X^A$  which will lead to parity violating X-interactions. Since there is no <u>a priori</u> reason (theoretically or experimentally<sup>9</sup>) for the interactions in the X-sector to be parity conserving, we allow this possibility also.)

We wish to emphasise that in renormalizable gauge theories there are restrictions on the choices of  $\,q_{_{\rm II}}\,$  and  $\,q_{_{\rm II}}\,$  due to the interplay between the weak and strong gauge groups. For example, with non-chiral strong gauge-groups and the type of unification schemes considered in Ref. 2, e can be coupled via X to either the n-quark or the  $\lambda$ -quark, but not to both (see Appx. I). We refer to these two situations (e coupled to n or  $\lambda$ ) as electron being "non-strange" or "strange" respectively. Also (if µ and e belong to the same Fermion multiplet)  $\mu$  will couple to the  $\lambda$ -quark, where e couples with n and vice versa. (In other words, if e is "strange",  $\mu$ is not). If, on the other hand, e and µ belong to different Fermionic multiplets (as is the case of the variant model, of Appx. I), But in no case can e and µ couple via both e and  $\mu$  may be "strange". the X's to the proton-quark or the charmed quark without conflicting with the charge and isospin assignments in our gauge models. In the sequel, though our discussion is phenomenological, we abstract the features of the X-interaction from gauge-theory considerations. As will be seen, this leads to important

-3-

experimental differences from other models 10 recently proposed in the literature. In summary, we consider the following three possibilities 11 for the choices of  $q_{\mu}$  and  $q_{\mu}$ :

- (i)  $(q_e, q_{\mu}) = (n, \lambda); e^{-non-strange}, \mu^{-strange};$
- (ii)  $(q_{\rho}, q_{\mu}) = (\lambda, n); \mu$  non-strange, e strange;
- (iii)  $(q_e, q_\mu) = (\lambda, \lambda')$  (such a possibility arises in the so-called prodigal model see Appx.I). Both  $e^-$  and  $\mu^-$  strange.

## Effective 4-Fermion interaction; heavy-X-case

In addition to quark mass, two important parameters in the model are the square of the coupling constant  $(f^2)$  and  $m_{\chi}^2$ . Two typical cases arise: 1)  $f^2/4\pi$  is small (perhaps as small as  $\approx 10^{-2}$ ); in this case, in order to account for the  $e^-e^+$ -annihilation data, X ought to be "light"  $(M_{\chi} \approx 15-30 \text{ BeV}, \text{ say})$ . The  $m_{\chi}^2$  may be exceeded in energy by the next generation of experiments. We refer to this as the <u>light-X-case</u>  $(m_{\chi}^2 \sim s)$ . 2)  $f^2$  is large  $(f^2/4\pi \sim 1)$ ; in this case X ought to be heavy  $(m_{\chi} \approx 100 \text{ BeV})$  to account for the  $e^-e^+$ -annihilation data (see estimates later). In this case s (and t)  $< m_{\chi}^2$ . We refer to this as the <u>heavy-X-case</u>, although in Sec.III.2 we briefly consider the case of a light-X-mass. [From the gauge theory point of view, both cases may be permissible, see remark in Appx.I.]

For s and t  $< m_X^2$ , one may treat the effective current-currentinteraction mediated by the X's as a local 4-Fermion interaction, which for the sequence of cases mentioned above reads as follows, after a Fierzreshuffle has been affected.

I) Parity-conserving case  

$$\begin{pmatrix} (X_{i}^{V})_{i} = e, \mu & \text{and} & (X_{i}^{A})_{i} = e, \mu & \text{are distinct fields with} & f_{i}^{V} = \pm f_{i}^{A} \equiv f_{i} \end{pmatrix}$$

$$\mathcal{L}_{X}^{\text{eff}} = \begin{pmatrix} \frac{f_{e}^{2}}{2} \\ \frac{m}{X_{e}^{V}} \end{pmatrix} \begin{pmatrix} \frac{1}{4} \end{pmatrix} \begin{bmatrix} -4 & s_{e} & s_{q_{e}} + 2 & V_{e} & V_{q_{e}} + 2 & A_{e} & A_{q_{e}} - 4 & P_{e} & P_{q_{e}} \end{bmatrix}$$

$$+ \begin{pmatrix} \frac{f_{e}^{2}}{2} \\ \frac{m}{X_{e}^{A}} \end{pmatrix} \begin{pmatrix} \frac{1}{4} \end{pmatrix} \begin{bmatrix} 4 & s_{e} & s_{q_{e}} + 2 & V_{e} & V_{q_{e}} + 2 & A_{e} & A_{q_{e}} - 4 & P_{e} & P_{q_{e}} \end{bmatrix}$$

$$+ (e \neq \mu)$$

II) Parity-non-conserving case

interactions, respectively.

$$(X_{i}^{V} \text{ and } X_{i}^{A} \text{ are identical fields}^{12}) \text{ with } f_{i}^{V} = \pm f_{i}^{A} \equiv f_{i})$$

$$\mathcal{L}_{\mathbf{X}}^{\prime} \stackrel{\text{eff}}{=} \begin{bmatrix} \frac{1}{2} \\ \frac{1}{m_{\mathbf{X}}} \\ e \end{bmatrix} \begin{bmatrix} \mathbf{V} & \mathbf{V} \\ \mathbf{e} & \mathbf{q} \\ \mathbf{e} & \mathbf{e} & \mathbf{e} \\ \mathbf{e} & \mathbf{e} & \mathbf{q} \\ \mathbf{e} & \mathbf{e} & \mathbf{e} \\ \mathbf{e} & \mathbf{e} \\$$

(2)

Here  $S_e$ ,  $V_e$ ,  $A_e$  and  $P_e$  denote the bilinear lepton covariants  $\{\overline{e} (X)\Gamma_i e(X)\}$  with  $\Gamma_i = 1$ ,  $\gamma_{\mu}, i\gamma_{\mu}\gamma_5$  and  $\gamma_5$  respectively. Similarly for the quark covariants  $S_{q_e}$ ,  $V_{q_e}$ ,  $A_{q_e}$  and  $P_{q_e}$ . The equality relations between  $f_{e,\mu}^V$  and  $f_{e,\mu}^A$  for I and II are suggested by various variants of gauge models. Note that the <u>overall sign</u> of the above effective interaction is fixed in <u>gauge</u> <u>models</u>, since it is a consequence of a basic vector-type Yukawa interaction. This will result in the sign of the interference term between the X and the photon-mediated amplitudes (in  $e^-e^+$  annihilation and  $e^\pm$  p-scatterings, for example) being fully determined.

Under I), we consider two typical possibilities:

(IA) Mass of the axial vector meson  $X^A$  is much larger than that of the vector meson  $X^V$ , so that we may drop the axial-contribution. Alternatively, vector-mass much exceeds so that we may drop the vector-contribution. The two cases lead to identical results for all our considerations, since they differ only in the signs of  $S \stackrel{S}{e} S_{e}$  and  $P \stackrel{P}{e} q_{e}$  terms, and these terms do not interfere with any equal to the contributions. We refer to the two cases as "vector-X" and "axial-X"

(IB) Vector and axial masses are equal; in this case one has an effective . (VV + AA) interaction before and after Fierz-reshuffle with no net S and P terms. (Consequences of the intermediate situation  $m_{\chi A}$  being comparable to  $m_{\chi V}$  can, of course, be worked out from the formulae appearing in the text.) In summary, then we have three cases to consider:

- (IA) "vector-X" or "axial-X"; effective interaction  $\frac{1}{2}$ (VV+AA) ± (SS+PP),
- (IB) (VV + AA) effective interaction, and
- (II)  $(V \pm A)(V \pm A)$  effective interaction.

For all three cases, only one X-mass is relevant for "low" energy X-interactions involving the electron and similarly the muon and the superscripts V and A may therefore be dropped. The strength of such interactions may thus be characterized by the <u>two positive parameters</u>  $\varepsilon_{e,\mu}$  defined by:

$$a_{X_{i}} \equiv (f_{i}^{2}/4\pi)(1/m_{X_{i}}^{2}) \equiv (\alpha \epsilon_{i})/(BeV)^{2} \qquad (i = e, \mu) , \qquad (4)$$

where  $\alpha = e^2/4\pi = 1/137$ . From now on we drop the subscript i also, as we consider processes involving the electron only; muon-processes can be obtained by simple substitutions  $\varepsilon_e \neq \varepsilon_u$ ,  $q_e \neq q_u$ .

### III.1 ELECTRON-POSITRON ANNIHILATION; HEAVY-X-CASE

The contributions of one-photon and the X-interaction (for  $s \ll m_{\chi}^2$ ) to the cross-section for  $e^{-e^+}$  annihilation into hadrons are in general given by:

$$\sigma_{h}(s) = \frac{4\pi s}{3} \left\{ \frac{\alpha^{2} \rho_{\gamma\gamma}(s)}{s^{2}} + \frac{2\alpha a_{\chi} \rho_{\gamma\chi}(s)}{s} + a_{\chi}^{2} \rho_{\chi\chi}(s) \right\},$$
(5)

where  $\rho_{\gamma\gamma}(s)$  and  $\rho_{\gamma\chi}(s)$  represent the hadronic tensors for the current correlations  $(V_{\mu}^{em} V_{\nu}^{em})$  and  $\frac{1}{2}(V_{\mu}^{em} V_{\nu}^{\chi} + V_{\mu}^{\chi} V_{\nu}^{em})$  respectively with  $V_{\mu}^{\chi} = \frac{1}{2}(V_{q})_{q}$ for case (IA) and  $(V_{q})$  for cases (IB) and (II). The function  $\rho_{\chi\chi}(s)$ represent the <u>sum</u> of contributions from the correlations  $(S_{q}S_{q}), (P_{q}P_{q}), (V_{q}V_{q})$  and  $(A_{q}A_{q})$  with appropriate coefficients, which may be worked out for the three cases from Eqs. (2) and (3).

If s is in the asymptotic region, dimensional considerations and scaling hypothesis suggest that all three functions  $\rho_{\gamma\gamma}(s)$ ,  $\rho_{\gamma\chi}(s)$  and  $\rho_{\chi\chi}(s)$ are essentially"constants". If, in addition, we assume the validity of lightcone hypothesis or parton model considerations, we may evaluate these constants for a given model <sup>13</sup> using the general formulae in Appx. II. For the case where the proton quark is not involved <sup>14</sup>, we obtain:

$$\rho_{\gamma X}(s) = -1 , \quad \rho_{XX}(s) = 6 , \quad (IA)$$

$$= -2 , \qquad = 6 , \quad (IB)$$

$$= -2 , \qquad = 12 , \quad (II)$$
while<sup>15</sup>, 
$$\rho_{\gamma \gamma}(s) = \sum_{i=1}^{n} Q_{i}^{2}$$
(6)

and  $|e|Q_i$  denotes the electric charge of the ith-type quark. Collecting the formulae (4), (5) and (6), we obtain 16 (for the heavy-X-case):

$$\sigma_{\rm h}(s) = \frac{4\pi\alpha^2}{3} \left[ \frac{\Sigma Q_{\rm i}^2}{s} - \begin{pmatrix} 1\\ 2\\ 2 \end{pmatrix} \varepsilon + \begin{pmatrix} 6\\ 6\\ 12 \end{pmatrix} \varepsilon^2 s \right]$$
(7)

with the three rows corresponding to the cases (IA), (IB) and (II), respectively. Note the <u>destructive interference</u> between electromagnetism and the vector-part of the X-interaction. This comes about because  $\mathcal{L}_X^{\text{eff}}$  or  $\mathcal{L}'_X^{\text{eff}}$  were derived from a basic vector-type Yukawa-interaction together with the fact that the electric charge of both n and  $\lambda$ -quarks is  $\frac{14}{3} - \frac{1}{3}|e|$ . The sign of the interference term is important in determining the magnitude of  $\varepsilon$  from the annihilation data.

We find that the reported data  $\frac{3}{16}$  for  $\sigma_{h}(s)$  with s varying from 9 to 25 (BeV)<sup>2</sup> can be fitted reasonably well in all three cases (IA, IB and II) with values of  $\varepsilon$  given in Table I and two typical values  $\frac{17}{160}$  for  $\Sigma Q_{\gamma}^{2}$ :

$$E Q_1^2 = 2 (3 \text{ triplets of fractional charges}),$$
  
=  $\frac{10}{3}$  (3 quartets of fractional charges).

(8)

These values of  $\Sigma Q_i^2$  are still compatible with <u>three quartets of integer charge</u> quarks, if we remark that when neither colour nor charm is excited

-7-

at SPEAR energies, then  $\Sigma Q_i^2 = 2$ , while if charm is excited but not colour, then  $\Sigma Q_i^2 = 10/3$ . (Note that the values of  $\varepsilon$  given in Table I are in the same range as suggested in Ref.4.)

	"Vector-X" (IA)	(VV + AA) <sub>eff</sub> (IB)	(V.± A)(V ± A) <sub>eff</sub> (II)
$\Sigma Q_i^2 = 2$	1/30	1/25	1/40
$=\frac{10}{3}$	1/50	1/40 to 1/50	1/50 to 1/60

## TABLE I Values of E from annihilation data

III.2 LIGHT-X-CASE

For a lighter X-mass  $(m_{\chi} \simeq 10-30 \text{ BeV})$ , the local 4-Fermi-approximation to the effective interaction would be completely inadequate as available centre-of-mass (energy)<sup>2</sup> s exceeds 50 (BeV)<sup>2</sup>. In this situation, the s (and t)dependence of  $e^{-e^{+}}$  hadrons will be strongly dependent on the "structure" of the matrix-element and the particular final state considered and one may no longer use the simple formula (7), which is valid exclusively for the heavy X-case  $(m_{\chi}^2 >> s,t)$ . Given the fact that we are dealing with a renormalizable theory, we remark that the s-dependence of the cross-section is not expected to be as steeply rising as for Eq. (7) when s approaches or exceeds  $m_{\chi}^2$ . (In fact, a variety of different complexions may arise depending upon the precise value of  $\sqrt{s}$  in relation to  $m_{\chi}$ ,  $m_q$  (quark-mass) and possibly other masses<sup>18</sup>) in the theory.) In summary, the lack of linear rise of the cross-section with s (at high s) is not to be taken as evidence against the possibility that the X-mechanism provides an explanation for the known  $e^{-e^{+}}$ -annihilation data.

From now on, we shall confine our discussions to the (simpler) heavy-X-case, since it allows us to make definite quantitative predictions. It should be remarked, however, that if the s-dependence is not as steep for the light X-case, as it is for the heavy X-case, the deviations of  $(e^+p/e^-p)$ ratio from unity and departures from scaling in ep-scattering would in general be less pronounced for a light-X than for the heavy-X for a given high  $s(=q^2)$ .

-8-

COMPARISON OF (e<sup>+</sup>p) VERSUS (e<sup>-</sup>p) AND ( $\mu^+p$ ) VERSUS ( $\mu^-p$ ) IN THE DEEP INELASTIC REGION

It was stressed in Ref. 4 that the interference between the vector (which arises from the electromagnetic as well as the X-interaction) and the axial-vector interaction (originating from the X-interaction only) should in general lead to a measurable difference between (e<sup>+</sup>p) and (e<sup>-</sup>p) cross-sections especially for large  $q^2 \ge \frac{1}{\epsilon}$ . Below we make a quantitative estimate of this

for the heavy-X-case difference  $\bigwedge$  assuming  $q_e = n$  or  $\lambda$  and making free use of the parton model hypothesis. The relevant formula for deep inelastic  $e^{\pm}p \rightarrow e^{\pm} + H$  crosssections for a general 4-Fermion interaction containing the covariants SS, PP, VV, AA, VA and AV is given in Appx.II. The ratio of  $(e^{\pm}p)$  and  $(e^{\pm}p)$  cross-sections for given values of incident lepton energy E, scattering angle  $\theta$  and momentum transfer square  $q^2$  is given by:

$$\frac{d\sigma^{e^{+}}(\mathbf{E},\theta,q^{2})}{d\sigma^{e^{-}}(\mathbf{E},\theta,q^{2})} = \frac{X_{+}}{X_{-}} , \qquad (9)$$

where 
$$X_{\pm}$$
 for our three cases (IA, IB and II) are given by:  

$$X_{\pm} = \begin{bmatrix} q_p^2 f_p(x) + q_n^2 f_n(x) + f_{q_e}(x) \left\{ -\frac{2}{3} \begin{pmatrix} \frac{1}{2} \\ 1 \\ 1 \end{pmatrix} \epsilon q^2 + \epsilon^2 q^4 \begin{pmatrix} \frac{1}{2} \\ 2 \\ 4 \end{pmatrix} \right\} \times (1 - y + y^2/2)$$

$$+ \begin{bmatrix} f_{q_e}(x) \epsilon^2 q^4 & \begin{pmatrix} \frac{1}{2} \\ 0 \\ 0 \end{pmatrix} \end{bmatrix} y^2$$

$$\pm \xi_{q_e} f_{q_e}(x) \left\{ -\frac{1}{3} \begin{pmatrix} \frac{1}{2} \\ 1 \\ 1 \end{pmatrix} \epsilon q^2 + \epsilon^2 q^4 \begin{pmatrix} \frac{1}{4} \\ 1 \\ 2 \end{pmatrix} \right\} y(2 - y) .$$
(10)

Here x and y are familiar kinematic variables defined in Appx.II;  $f_{p,n,\lambda}(x)$  denote the quark momentum distribution functions within the proton;  $\xi_{q_e} = \pm 1$  for quarks and  $\pm 1$  for anti-quarks. In (10) we have not exhibited the anti-quark contribution nor the  $\lambda$ -quark-contribution in  $\Sigma Q_{if_i}^2(x)$ , since the anti-quark and  $\lambda$ -quark distribution functions are negligible (less than 5%) compared with those of the p and n-quarks at  $x \ge 0.2$  (i.e.  $\omega < 5$ ). Note, however, that the anti-quark

-2-

IV.

contributions systematically tend to <u>reduce</u> the difference between  $(e^{\dagger}p)$  and  $(e^{-}p)$ -scatterings. This is because, on the one hand, they increase the symmetric term (given by the first two brackets) and on the other, they decrease the asymmetric term (the last term in Eq. (10)) due to the  $\xi_q$ -factor.

Following the same reasoning, we note that the ratio  $(X_{+}/X_{-})$  is expected to stay near unity for all values of  $q^2$  in the event the electron is strange (i.e.  $q_e = \lambda$ ); since in this case, assuming that  $f_{\lambda}(x) = f_{\overline{\lambda}}(x)$ within the proton for all x, the contribution of  $\lambda$ -quark to the last term in Eq. (10) is cancelled by that of the  $\overline{\lambda}$ -quark.

On the other hand, if the electron is non-strange (i.e.  $q_{i} = n$ ), the ratio  $(X_X)$  would differ from unity for all  $q^2 \neq 0$ , since the neutron and anti-neutron-quark distributions within the proton are very different from each other. The precise deviation from unity however, depends sensitively on the ratio  $f_p(x)/f_n(x)$ . The kinematic region of interest at which deviations from unity would be appreciable corresponds to high  $|q^2| \ge 10 (BeV)^2$  and,therefore, low  $\omega \leq 5$  given that the energy E of the incident lepton at which the SLAC experiment<sup>6)</sup> is performed is 13.9 BeV. For such low  $\omega$  (especially for  $\omega < 2$ , which is appropriate for  $q^2 \approx -15 (BeV)^2$ ), the functions  $f_p(x)$  and  $f_n(x)$  as well as their ratio vary rapidly leaving room for considerable Available information on  $f_{p}(x)/f_{n}(x)$ is given uncertainty. by the curves in Ref. 19, which are based on (ep) and (en) data as well as the fitting of the known sum rules. However, due to their rapidly varying nature, the precise numerical estimates of  $f_p(x)/f_n(x)$  for low  $\omega$  based on these estimates of the p (and therefore the deviations of  $(e^+p/e^-p)$  from unity) should be treated with some caution; only the qualitative trend may still be trusted. Be that as it may, we present in Table II values of (ep/ep) for the case of electron being non-strange(i.e. q<sub>e</sub> = n) at several points relevant to the SLAC experiment, taking  $(f_p/f_n)$  from Ref.19.

Preliminary experimental measurements <sup>6</sup> seem to indicate that the ratio  $(e^{\dagger}p/e^{-}p)$  is unity within  $\pm 10\%$  for  $q^2$  varying between 0 and  $-15 (BeV)^2$ . This appears to exclude possibilities (IB) and (II) for the case of electron being non-strange  $(q_e = n)$ . Case (IA) may still be acceptable, if we allow for the uncertainty in parton-model calculations together with the uncertainty in  $f_p(\omega)/f_n(\omega)$  for low values of  $\omega$ , the anti-quark contributions as well as the modifications due to 2-photon contribution to  $e^{\pm}p$ -scatterings. However, if the experiments preserve the present trend for high  $|q^2|$  ( $\simeq 25$  (BeV)<sup>2</sup>)

-10-

and  $\omega > 1.5$ , even case (IA) (with  $q_e = n$ ) may be ruled out. This would be leave us with the only possibility that electron is strange (i.e.  $q_e = \lambda$ ).

Our remarks for the ratio  $(e^{\dagger}p/e^{-}p)$  apply equally well to the ratio  $(\mu^{\dagger}p/\mu^{-}p)$  if we substitute  $\varepsilon_{e} \rightarrow \varepsilon_{\mu}$  and  $q_{e} \rightarrow q_{\mu}$ . Thus, a comparison of  $e^{\dagger}p$  versus  $e^{-}p$  and  $(\mu^{\dagger}p)$  versus  $(\mu^{-}p)$  at high  $|q^{2}|$  would be most helpful in deciding if either the electron or the muon may be coupled to the newtron-20) quark via X with an effective strength<sup>21)</sup> of order  $\alpha(2 \times 10^{-2})$  BeV<sup>-2</sup>.

## TABLE II

$$\frac{\sigma^{e^{-p}}(E = 13.9, a^2, \theta = 50^c)}{\sigma^{e^{-p}}(E = 13.9, a^2, \theta = 50^c)}$$

for the heavy-X-case  $(m_X^2 \gg s,t)$  with electron being non-strange.(If electron is strange, the above ratio is expected to be unity for all values of  $q^2$ .) The entries shown are for  $\epsilon = 1/50$ . Values of  $q^2$  and E. are units of (BeV).

	q <sup>2</sup> = -5	$q^2 = -10$ .	q <sup>2</sup> = -15	q <sup>2</sup> = -20
ω ≃	5.0	2.42	1.54	1.18
$f_{p}(\omega)/f_{n}(\omega)$	1.8	2.0	3.6	6.0
IA(q <sub>e</sub> = n) "vector-X"	<u>e</u> = 1.08 e	1.16	1.18	1.15
$IB(q_e = n)$ (VV + AA) <sub>eff</sub>	$\frac{e^+}{e^-} = 1.19$	1.42	1.43	î.42
$II(q_e = n)$ $(V \pm A)(V \pm A)_{eff}$	$\frac{e^+}{e^-} = 1.23$	1.57	1.63	1,65

-11-

V. APPARENT DEVIATIONS FROM SCALING IN  $(e^{\pm}p)$  AND  $(\mu^{\pm}p)$ -SCATTERINGS As mentioned in Ref. 4, the replacement of  $1/q^2$  photon-like propagator by a constant  $(\frac{-1}{m_{e}^2})$  in the X-contribution to the scattering

amplitude would reflect itself in an apparent violation of scaling in deep inelastic ep(or µp)-scattering, even though intrinsic scaling may hold in the structure functions involving quark densities (such as  $(V^{em}V^{em})$ , (V V ), (A A ),  $(V^{em}A )$ , (V A ) and (S S ) etc.) The theoretical  $q_e q_e$   $q_e q_e$   $q_e q_e$   $q_e q_e$  formula for the cross-section  $d^2\sigma/dxdy$  for ep-scattering in the presence of axial-vector and vector-interactions is given by:

$$\frac{d^{2}\sigma}{dx dy} = \frac{4\pi\alpha^{2}s}{q^{4}} \left[ (1-y) vW_{2}(q^{2},v) + xy^{2} m_{p} W_{1}(q^{2},v) - xy(1-y/2) vW_{3}(q^{2},v) \right], (11)$$

where  $s = (p + k)^2$ ,  $x = \frac{1}{\omega} = -(q^2/2m_N v)$ ,  $y = (\frac{p \cdot q}{p \cdot k})$  and

 $v = (p,q)/m_N = (E - E')$ . The quantities p and k denote the 4-momenta of the incoming nucleon and lepton respectively, while q is the 4-momentum transfer between the incoming and the outgoing lepton. Note the appearance of the  $vW_3$  term due to (vector-axial-vector) density correlation (analogous to the case of neutrino-nucleon scattering). The parton model formulae for the functions  $vW_{2,3}$  and  $M_NW_1$  for our three cases (IA, IB and II) are given by:

$$vW_{2}(\mathbf{x},\mathbf{q}^{2}) = \mathbf{x} \left[ \sum_{i} Q_{i}^{2} \mathbf{f}_{i}(\mathbf{x}) + \mathbf{f}_{q}_{e}(\mathbf{x}) \left\{ \mathbf{q}^{4} \begin{bmatrix} \varepsilon^{2}/4 \\ 2\varepsilon^{2} \\ 4\varepsilon^{2} \end{bmatrix} + \mathbf{q}^{2}(Q_{q}) \begin{bmatrix} \varepsilon \\ 2\varepsilon \\ 2\varepsilon \end{bmatrix} \right\} \right]$$
$$\equiv \mathbf{x} \left[ \sum_{i} Q_{i}^{2} \mathbf{f}_{i}(\mathbf{x}) + \Delta_{2}(\mathbf{q}^{2},\omega) \right]$$

$$MW_{1}(\mathbf{x},\mathbf{q}^{2}) = \frac{1}{2} \left[ \sum_{i} Q_{i}^{2} \mathbf{f}_{i}(\mathbf{x}) + \mathbf{f}_{q_{e}}(\mathbf{x}) \mathbf{q}^{4} \begin{pmatrix} \varepsilon^{2} \\ 0 \\ 0 \end{pmatrix} \right]$$
$$= \frac{1}{2} \left[ \sum_{i} Q_{i}^{2} \mathbf{f}_{i}(\mathbf{x}) + \Delta_{1}(\mathbf{q}^{2},\omega) \right]$$
$$vW_{3}(\mathbf{x},\mathbf{q}^{2}) = \pm 2\mathbf{f}_{q_{e}}(\mathbf{x}) \left\{ Q_{q_{e}} \mathbf{q}^{2} \begin{pmatrix} \varepsilon/2 \\ \varepsilon \\ \varepsilon \end{pmatrix} + \mathbf{q}^{4} \begin{pmatrix} \varepsilon^{2}/4 \\ \varepsilon^{2} \\ 2\varepsilon^{2} \end{pmatrix} \right\}$$

-12-

(12)

The three rows correspond to the cases (IA), (IB) and (II) respectively. The sum i runs over p, n and  $\lambda$ ;  $|e|Q_1$  denotes the electric charge of the ith quark and  $f_1(x)$ , as before, denotes the i-type quark momentum distribution function inside the proton. The factor  $\xi_{q_e}$  is +1 for quark-parton contribution and it is -1 for anti-quark-parton contribution. The  $\pm$  signs in Eq.(12) correspond to  $e^{\pm}$  p-scatterings. Note that the new terms, which arise in the presence of X-interaction, are proportional to  $f_{q_e}(x)$ , where  $q_e(x)$  is  $\lambda$  or n, depending upon whether the electron is strange or non-strange. these terms depend upon  $q^2$  and  $q^4$  and thus provide the scale non-invariant contributions to  $VW_2$  and  $MW_1$ . The measure of the deviations from scaling in these two functions is given by

(13)

$$D_{1,2}(q^2,\omega) \equiv \frac{\Delta_{1,2}(q^2,\omega)}{\Sigma Q_i^2 f_i(x)}$$

where  $\Delta_{1,2}$  are defined through Eq.(12).

Since  $\epsilon$  is small  $(\approx \frac{1}{50})$ , it follows that  $D_{1,2}(q^2,\omega)$  will be appreciable only for large  $|q^2| \ge 15$  (BeV)<sup>2</sup>. This, however, corresponds to small  $\omega$  (<2.5) at SLAC energies. For such values of  $\omega$ , it is easy to see that  $\underline{D}_{1,2}(\underline{q^2},\omega)$  would be less than or of order 5% for  $|\underline{q}^2| < 25$  (BeV)<sup>2</sup> in the event the electron is strange  $(\underline{q} = \lambda)$ . This is because the functions  $D_{1,2}(\underline{q}^2,\omega)$  are proportional to  $f_{\underline{q}_e}(x)$  and the strange-quark content function  $f_{\lambda}(x)$  is at least an order of magnitude smaller than the non-strange quark content functions  $f_p(x)$  and  $f_n(x)$  within the proton for  $\omega < 4$ . These remarks hold for all three cases (IA), (IE) and (II).

If, on the other hand, the electron is non-strange (i.e.  $q_{\theta} = n$ ), one would in general expect to see significant violation of scaling for large  $|q^2| \ge 20 (\text{BeV})^2$ . The precise value of such violation depends sensitively on the ratio  $f_p(x)/f_n(x)$ . As remarked earlier in connection with the comparison of (e<sup>+</sup>p) versus (e<sup>-</sup>p), this ratio does not seem to be well relevant known for small values of  $\omega < 2$ . This is the value which is/for large  $|q^2| \ge 20$ at SLAC energies. Once again, we estimate the degree of violation for different values of  $q^2$  by taking  $f_p(x)/f_n(x)$  from Ref. 19 and list the corresponding numbers in Table. III. We should stress that the precise numer-

-13-

ical estimates may not be taken seriously, although the qualitative trend of increasing deviations from scaling with increasing  $|q^2|$  and the effects for the  $vW_2$ -function being large for cases (II) and (IB) compared with (IA), can be trusted.

#### TABLE III

Scaling violations for the case of electron being non-strange  $(q_e = n)$ ; with some typical values of  $\omega$  and  $\varepsilon = 1/50$ . (If e is strange, violation of scaling is much less than 5% for  $|q^2| < 25 (BeV)^2$  and  $\omega < 4$ .)

	ω	$\frac{f_{p}(\omega)}{f_{n}(\omega)}$	vector-X (IA)( $q_e = n$ )		(VV+AA (IB)(q <sub>e</sub>	) eff = n)	(V±A) ( (II)(q <sub>e</sub>	V <sup>±A)</sup> eff = n)
			Dl	, D <sub>2</sub>	D <sub>1</sub>	, D <sub>2</sub>	Dl	<sup>1</sup> D <sub>2</sub>
q <sup>2</sup> = -15	2	2.6	0.07	1 2 0.09	Ö	0.28	0	1 1 0.40 1
q <sup>2</sup> = −25	1.5	3.6	0.14	0.13	0	0.50	0	1 1 0180

To summarize:

1) Despite the presence of scalar and pseudoscalar interactions for case (IA) (corresponding to either "vector-X" or "axial-X"), the deviations from scaling in  $MW_1(q^2, v)$  are tolerable in the presently available kinematic region for ep scattering. This differs from the conclusion drawn in Ref.19, where large deviations from scaling are noted in the presence of scalar interactions. Large part Such a difference is in  $\bigwedge$  due to the fact that all three quarks (p,n and  $\lambda$ ) are assumed to share the anomalous interaction with equal strength in Ref.19, while only the neutron or the  $\lambda$ -quark is involved in the anomalous interaction for our case.

2) While the above estimates are given for (ep)-scattering, the deviations from scaling will be enhanced considerably for (en)-scattering compared with (ep)-scattering in the event that electron is non-strange  $(q_e = n)$ . This is because of the larger n-quark content compared with the p-quark content within the neutron relative to the proton. Of course, if the electron is strange, the effects are equally suppressed for (en)-scattering as is the case for (ep)-scattering.

-14-

3) A characteristic feature of Eq.(12) is that the functions  $VW_2$ ,  $VW_3$  (for e) and  $MW_1$  must increase with  $|q^2|$  for all  $q^2$  and fixed  $\omega$ . This is because the interference terms in  $VW_2$  and  $VW_3$  (being proportional to  $(q^2 Q_q)$ ) are necessarily constructive for space-like  $q^2 < 0$  and

 $Q_{q_e} = -\frac{1}{3}$  corresponding <sup>14</sup> to the electron being coupled to either the n or the  $\lambda$  quark via X .

4) The entries in Table III indicate that deviations from scaling in the  $VW_2$  function are excessive for case (II) and case (IE) with  $q_e = n$ . This appears to be inconsistent with the (ep)-data which seems to assert that scaling holds within 10-15 %. However, it may not be easy to draw clear-cut conclusions unless one re-analyses <sup>22)</sup> the data in terms of  $W_1$ ,  $W_2$  and  $W_3$  functions (Eq.(11)). We feel that such an analysis of the data is worth-while not only in view of testing the possibility of additional interactions as considered here, but also to estimate<sup>23)</sup> the 2-photon contribution.

5) If the electron is strange  $(q_e = \lambda)$ , the contribution of the  $\forall W_3$ term vanishes if  $f_\lambda(x) = f_{\overline{\lambda}}(x)$  for all x. This is because the  $\lambda$ -quark contribution to the  $\forall W_3$  term is cancelled by the anti- $\lambda$ -quark contribution due to the  $\xi_{q_e}$  factor in Eq.(11). In this case the data may be analysed only in terms of the  $\forall W_2$  and  $MW_1$  functions. The deviations from scaling for these two functions are small (less than 5%) in the presently available kinematic region, since  $f_\lambda(x)/f_{p,n}(x)$  is small for low  $\omega$  (< 3). However, such deviations should increase with  $\omega$  for a fixed high  $|q|^2 \ge 20 (BeV)^2$  as  $\omega$  increases between 3 and 10, since the ratio  $f_\lambda(x)/f_{p,n}(x)$  rises <sup>19</sup> rapidly in this region.

6) The remarks made here with regard to (ep)-scattering apply also to (µp)experiments scattering/being carried out at FNAL with the substitutions  $\varepsilon_e \rightarrow \varepsilon_{\mu}$  and  $q_e \rightarrow q_{\mu}$ . It is worth noting that the higher w-values (together with high  $|q^2|$  values) available in this case (due to high incident energies) are useful to avoid uncertainty in theoretical estimates stemming from the uncertainty in  $f_p(\omega)/f_n(\omega)$ . This applies both to the comparison of  $(\mu^+p)$  versus  $(\mu^-p)$  (Sec.IV) and to deviations from scaling in (µp)-scattering. In view of remark 5), it is especially interesting to verify whether deviations from increasing scaling, if any, rise in this case with  $\int_{k} \omega$  for a fixed high  $|q^2|$ . If this effect is observed, it may be inferred that the muon is "strange".

-15-

## VI. HYPERFINE STRUCTURE

Due to the presence of axial interactions of the form,  $(A_e^A_q)$  in all

three cases (IA, IB and II), the X-interaction will contribute to hyperfine splitting in hydrogen, which is given by:

$$\frac{hv_{hfs}}{v_{hfs}} = (1000) \begin{pmatrix} \varepsilon/2 \\ \varepsilon \\ \varepsilon \end{pmatrix} g_{q_e}^A \quad \text{parts per million} , \qquad (14)$$

where

$$g_{q_e}^{A} \overline{u}_{p} i\gamma_{\mu}\gamma_{5} u_{p} \equiv \langle P | \overline{q}_{e} i\gamma_{\mu}\gamma_{5} q_{e} | P \rangle \qquad (15)$$

If the electron is strange  $(q_e = \lambda)$ , we expect  $g_{q_e}^A \simeq 0$ , so that the above

contribution is well within the theoretical uncertainty  $^{26)}$  of about 4 to 6 parts per million (in magnitude).

If electron is non-strange  $(q_e = n)$ , the extent to which the above contribution may pose a restriction depends on the magnitude of  $g_q^A$  with

 $q_e = n$ . If one accepts the value  $g_q^A = (1 - g_A^\beta) = (1 - 1.2) = -0.2$ , for  $q_e = n$ , as suggested in Ref. 9, we obtain (setting  $\epsilon \simeq 1/50$ )

 $e^{-1}$ , as suggested in Ref. 9, we obtain (setting  $\epsilon \simeq 1/50$ )

 $\frac{\Delta v_{hfs}}{v_{hfs}} = - \begin{pmatrix} 2\\ 4\\ 4 \end{pmatrix} \quad \text{parts per million} , \quad (16)$ 

which is still compatible with the theoretical uncertainty mentioned above. Thus hfs considerations do not, at present experimental and theoretical accuracy, rule out the possibility of a non-strange electron. (For the strange electron, of course, there never was any problem.)

-16-

VII.  $\pi^0 + e^+e^-$ ,  $\eta + \mu^+\mu^-$  AND  $\eta + e^+e^-$ -DECAYS

The X-interaction will in general contribute to  $\pi^0 + e^+ e^-$ ,  $\eta + \mu^+ \mu^-$  and  $\eta + e^+ e^-$ -decays. Even though the X-contribution is expected to be of the same order as the 2-photon contribution (since  $\alpha \epsilon = \mathcal{O}(\alpha^2)$ , the rate of  $\pi^0 + e^+ e^-$ -decay for case (IA) (with "vector-X") is in general expected to be enhanced compared with the cases (IB) and (II) as well as the 2-photon case by a factor  $(m_\pi/m_e)^2$  assuming that the matrix elements are of the same order in all cases. This is due to the presence of <u>pseudoscalar</u> effective interaction for case (IA), which is absent in all other cases. Below we estimate the rates.

# $\pi^{0} \rightarrow e^{+}e^{-}$ decay:

If the electron is strange  $(q_e = \lambda)$ , the X-contribution to  $\pi^0 \rightarrow e^+e^-$ -decay is suppressed in all three cases (IA, IB and II), since  $(\overline{\lambda}\lambda)$  is isoscalar while  $\pi^0$  is isovector.

Thus X-contribution to  $\pi^0 \rightarrow e^+e^-$ -decay would be significant <u>only</u> provided the electron is non-strange  $(q_e = n)$ . The rates for the X-contribution in the different cases are given by:

Case (IA) ("vector-X"  $(\frac{1}{2}(VV+AA) - (SS+PP))$ )-effective interation)

$$\Gamma(\pi^{0} \rightarrow e^{+}e^{-}) = \frac{(f^{2}/m_{\chi}^{2})^{2}}{16\pi m_{\pi}^{3}} [f_{\pi}^{2} m_{e}^{2} + h_{\pi}^{2} m_{\pi}^{2}] (m_{\pi}^{2} - 4m_{e}^{2})^{2}$$
(17a)

$$\simeq \frac{(r^2/m_{\chi}^2)^2}{16\pi} \left(\frac{h_{\pi}}{m_{\pi}}\right)^2 m_{\pi}^5$$
(17b)

Cases (IB) and (II) ((VV + AA)-effective and (V ± A)-chiral)

$$\Gamma(\pi^{0} + e^{+}e^{-}) = \frac{(f^{2}/m_{\chi}^{2})^{2}}{4\pi m_{\pi}^{3}} [f_{\pi}^{2} m_{e}^{2}] (m_{\pi}^{2} - 4m_{e}^{2})^{2}$$

$$\simeq \frac{(f^{2}/m_{\chi}^{2})^{2}}{4\pi} m_{\pi}^{3} m_{e}^{2} , \qquad (18)$$

where the constants  $\mathbf{f}_{\pi}^{}$  and  $\mathbf{h}_{\pi}^{}$  are defined by:

$$\langle 0|\overline{q}_{e} i\gamma_{\mu}\gamma_{5} q_{e}|\pi^{0}\rangle \equiv if_{\pi} p_{\pi\mu} \frac{1}{(2\pi)^{3/2}} (2E_{\pi})^{-\frac{1}{2}}$$

and

$$\langle 0 | \overline{q}_{e} \gamma_{5} q_{e} | \pi^{0} \rangle \equiv i h_{\pi} m_{\pi} \frac{1}{(2\pi)^{3/2}} (2E_{\pi})^{-\frac{1}{2}}$$
 (19)

In going from Eq.(17a) to Eq.(17b), we have dropped the  $m_e^2$  term. We have also <u>assumed</u> both for (17b) and (18) that  $f_{\pi}$  is of the same order as the  $\pi \neq \mu\nu$  decay constant, i.e.  $f_{\pi} \sim m_{\pi}$  for  $q_e = n$ , which seems reasonable. Substituting  $(f^2/4\pi)m_X^{-2} \approx (\alpha/50)$  BeV<sup>-2</sup> in the above formulae, we obtain the following branching ratios:

$$\frac{\Gamma(\pi^{0} \rightarrow e^{+}e^{-})}{\Gamma(\pi^{0} \rightarrow 2\gamma)} \simeq \left(\frac{h_{\pi}}{m_{\pi}}\right)^{2} (5 \times 10^{-4}) \qquad (IA)$$

$$\simeq 2.5 \times 10^{-8} \qquad (IB \text{ and } II) \qquad (20)$$

for the case of non-strange electron. A recent review of the data appears to set an upper limit of 8 x  $10^{-6}$  for the above branching ratio at 90% confidence This is certainly consistent with cases (IB) and (II); but it excludes level. case (IA) ("vector-X") with non-strange electron, if  $h_{\pi} \circ f_{\pi} \circ m_{\pi}$ . This is presumed to be the case by many authors (see, for example, Refs. 24 and 28). However, the constant  $h_{\pi}$  need not be as large as  $f_{\pi}$ . For example, if one uses the field equations to equate the pseudoscalar quark density  $P_{q}$ with  $(1/2m_{a})(\partial_{\mu}A^{q})$  where  $m_{a}$  is the quark mass, then one obtains  $h_{\pi} = (m_{\pi}/2m_{q}) f_{\pi}$ , which may comfortably be of order (f<sub> $\pi$ </sub>/10) for even a moderately heavy quark. Because of this uncertainty in the estimate of h\_ we conclude that  $\pi^0 \rightarrow e^+e^-$ -decay does not as yet yield decisive information to choose between the cases (IA), (IB) and (II) even for the non-strange quark case, although lowering of the branching ratio to the level  $10^{-7}$  should disfavour case (IA) (with  $q_e = n$ ). If the electron is strange,  $\pi^0 \rightarrow e^+e^-$ -decay is not sensitive to the anomalous interaction in any case.

## $\eta \rightarrow \ell + \overline{\ell} - \text{decays} (\ell = e, \mu)$

In contrast to  $\pi^0$ -decay, where  $(\lambda\overline{\lambda})$  density does not contribute, for  $\eta$ -decay such densities are important. Thus  $\eta$ -decay is sensitive to both strange and non-strange lepton possibilities. Of course the absolute rate

-18--

is again suppressed for cases (IB) and (II) compared with case (IA) (if the matrix elements are of the same order) just as for  $\pi^0 \rightarrow e^+e^-$ -decay. The contributions to  $\eta \rightarrow l\bar{l}$  decay (l = e or  $\mu$ ) (using the formulae for  $\pi^0$ -decay with the substitution  $\pi \rightarrow \eta$ ) are given by <sup>29</sup>)

$$\Gamma(\eta \rightarrow e^+e^-) \simeq (h_{\eta}/m_{\eta})^2$$
 (3 eV) (IA)  
 $\simeq (f_{\eta}/m_{\pi})^2$  (2 x 10<sup>-7</sup> eV) (IB and II)

(21)

$$\Gamma(\eta \neq \mu^{+}\mu^{-}) \simeq (h_{\eta}/m_{\eta})^{2} \quad (2.1 \text{ eV}) \qquad (IA)$$

$$\simeq (f_{\eta}/m_{\pi})^{2} \quad (6 \times 10^{-3} \text{ eV}) \quad (IB \text{ and } II) \qquad (22)$$

The constants  $f_{\eta}$  and  $h_{\eta}$  are defined in the same manner as  $f_{\pi}$  and  $h_{\pi}$  with the substitution  $\pi \rightarrow \eta$  in Eq.(19). One may expect (barring selection rules) that  $f_{\eta}$  is nearly equal to  $f_{\pi}$ , which in turn is of the same order as  $\pi \rightarrow \mu + \nu$ -decay constant; thus  $f_{\eta} \sim m_{\pi}$  (within a factor of 2 or 3). On the experimental side,  $30^{\circ}$  there is no number quoted for the  $\eta \rightarrow e^+e^-$ -decay; while  $\Gamma_{exp}(\eta \rightarrow \mu^+\mu^-) \approx 0.057 \text{ eV}$ . This latter number is certainly consistent with cases (IB) and (II) (for either strange or non-strange lepton). The consistency for case (IA) depends upon whether  $(h_{\eta}/m_{\eta})$  may be as small as (1/10) or not. [Note, if we replace the pseudoscalar quark-density  $P_q$  by  $(1/2m_q)(\partial_{\mu}A_{\mu}^q)$ , we obtain  $(h_{\eta}/m_{\eta}) \approx (m_{\pi}/2m_{q})$ .]

In summary, the leptonic decay modes of  $\pi^0$  and the partible with cases (IB) and (II) (with either strange or non-strange lepton) and with case (IA) for strange leptons; the compatibility with case (IA) for non-strange lepton is not easy to judge (under the present theoretical and experimental accuracy) due to uncertainty in the estimates of  $h_{\pi}$  and  $h_{\eta}$ . In view of the possible existence of the anomalous interactions, a search for  $\pi^0 \neq e^+e^-$  and  $\pi \neq e^+e^-$ -decays at a level much higher than the 2-photon contribution would be helpful. [We should also urge for a search for  $\pi^0 \neq \mu e$  and  $\pi^0 \neq \mu e^-$  decays, as these decays arise in certain variants of our gauge models and would decide whether electrons and muons have the same or different "colours".]

-19-

VIII.

MASSIVE LEPTON-PAIR PRODUCTION IN p + p COLLISIONS AND  $p + p \rightarrow l + H$ 

The X-interaction will, in general, affect the production of lepton pairs in hadron-hadron collisions in a manner very similar to the production of hadrons in ( $e^- + e^+$ ) annihilation. The general dependence of the crosssection on the invariant lepton pair (mass)<sup>2</sup>  $M_{L\bar{L}}^2$  for the case of heavy X ( $M_{L\bar{L}}^2 \ll m_{\chi}^2$ ) is given by

 $\frac{d\sigma'' \text{photon} + X''}{d\sigma'' \text{photon}''} = 1 + \sigma(\epsilon)M^2 + \sigma(\epsilon^2)M^4, \quad ,$ 

where the terms of  $\theta(\varepsilon)$  and  $\theta(\varepsilon)^2$  can be determined  $^{32)}$  in a parton-model framework.

In view of the fact that recent experiments on  $p + p \rightarrow l^+ + l^- + H$  carried out <sup>33)</sup> at BNL and  $p + p \rightarrow l + H$  being carried out <sup>5)</sup> at FNAL and ISR seem to indicate that lepton production is as much as one to two orders of magnitude higher than what is expected on the basis of 1-photon diagram and parton model formulae, it is tempting to suppose that the same mechanism which is responsible for the anomalous behaviour of  $e^-e^+$ -hadrons, may also be responsible for the anomalously large production of lepton pairs. (Note that in the experiments which so far study  $p + p \rightarrow l + H$ , one does not yet know whether the observed lepton is associated with its anti-lepton. However, if the above explanation is to apply, this must be the case.)

Fitting of the data for some specific cases has been made recently by Soni  $^{24}$ . We may add the following remarks:

(1) If the produced lepton (e<sup>-</sup> or  $\mu^-$ ) is strange, the cross-section will be modified significantly compared with the 1-photon cross-section in a region which involves high  $q^2 = M_{\ell\bar{\ell}}^2$  and high  $\omega$ . (What is needed is that  $f_{\lambda}(\omega) f_{\bar{\lambda}}\left(\frac{s}{M_{\ell\bar{\ell}}^2 \omega}\right)$  be large, where  $s = invariant (energy)^2$  for the (p-p-system).)

(2) The lepton-pair produced via the X-interaction can, of course, be distinguished from that produced via the decay of vector mesons through the characteristic mass plot. (This latter mechanism has been suggested by many authors  $3^{4}$ ) as a possible explanation of the data.)

-20-

(3) We mention a third explanation. Assume that quarks carry integer charges and are not too heavy ( $m_q \approx a$  few BeV) and that they decay into (leptons + pions) with lifetimes of order  $10^{-12}$  to  $10^{-10}$  sec violating baryon and lepton number conservation. Such a possibility could arise as a limiting case within our gauge scheme <sup>2</sup>; without conflicting with the known stability of the proton. In this case, the supposedly large production of leptons may be attributed to the production of <u>real</u> ( $q + \bar{q}$ ) pairs with cross-section of order  $10^{-4}$  compared with pion-production (sufficiently above ( $q\bar{q}$ )-threshold) followed by decay of the quark to (lepton + pions). Similarly for the anti-lepton. With this mechanism, the production of a lepton need not always be associated with that of its anti-lepton. This provides a distinction from the other explanations. Furthermore, we expect (see Ref.2) the quark decays to be parity violating, i.e. the lepton to carry net helicity. Of course, for this explanation to hold, it is necessary that there is a threshold <sup>35</sup>

#### IX. CONCLUSIONS

The purpose of this paper is two-fold. A) First, to abstract, from the class of gauge models proposed <sup>1),2)</sup> to unify leptonic and baryonic phenomena, information about the types of allowed and forbidden couplings and their signs and to utilize this information in making predictions about magnitude and energy dependence of  $e^+ + e^- \rightarrow$  hadrons, deviations of  $(e^+p/e^-p)$ total cross-sections from unity, and apparent deviations from scaling in  $(e^+p)$  experiments. B) Second, we wish to show (and this is done in Appx.I) that the severe limitation on characteristic energy at which anomalous lepton-hadron interactions would manifest themselves imposed by our original basic gauge model - and which would have excluded SLAC energies as being low - can be relaxed and the masses of the exotic X-particles responsible for the anomalous interactions can be lowered, from being superheavy (> 10<sup>4</sup> BeV) as in the basic model to being just heavy ( $\approx 10^2$  BeV) or even light ( $\simeq 15 \sim 30$  BeV).

In respect of A), the most severe limitations which our gauge models impose is that X-mediated anomalous interactions NEVER permit a coupling of electrons to the proton-quarks or to the charmed

-21-

quarks, but only to neutron-quarks or to the  $\lambda$ -quarks (referred to as the cases of "non-strange" or "strange" electron, respectively). Identical restrictions apply to the anomalous coupling of the muon. This has significant consequences for all processes considered and leads to important quantitative differences between our predictions and those of other authors.

Further, we allow for the possibility of the X-particles being light (15 $\vee$ 30 BeV) and remark that this may have the effect that the anomalous cross-sections for  $e^+ + e^- \rightarrow$  hadrons do not rise so steeply with energy as is the case for the heavy X-particles ( $\simeq$  100 BeV). An analysis of present data (summarized in Table IV) with these points in mind, inclines one to the view that even though we cannot yet exclude the possibility of the electron being non-strange (particularly with a light X), the trend of the data is towards a "strange" character for the electron (and towards its neutrino being "charmed"). The strangeness attribute of the electron has experimental consequences - for example, one may predict a predominant production of  $\phi^0$ 's and  $\eta_1^0$ 's and possibly also (XK) in future  $e^+ + e^-$  experiments at higher SLAC energies.

On the theortical side in respect of constructing a variant model which should permit for a heavy or light X (instead of a superheavy X with mass >10<sup>4</sup> BeV, which would be irrelevant for SPEAR energies), we have succeeded (Appx.I), but at the unattractive price of doubling the number of Fermions (including quarks) in the new model. In view of the theoretical difficulties of constructing an attractive gauge model, we wonder if it is not the basic model - with its superheavy or heavy X - which is, after all, the model likely to be correct and that at SLAC energies the anomalous lepton-hadron interaction which we predicted is really inoperative. Future SLAC, NAL and ISR experiments involving both  $e^{\pm}$  and  $\mu^{\pm}$  may help confirm or remove such reservations.

#### ACKNOWLEDGMENTS

We thank E. Bloom, J. Ellis, G. Furlan, Riazuddin and especially C.H. Llewellyn Smith for innumerable helpful discussions. One of us (J.C.P.) wishes to thank the International Atomic Energy Agency and UNESCO for hospitality at the International Centre for Theoretical Physics, Trieste.

-22-

In this appendix we consider some of the gauge models of Ref.2 and the pattern of anomalous lepton-hadron interactions they give rise to. As remarked in Ref. 2, it is an inescapable conclusion of our gauge models which unite leptons and hadrons that these anomalous interactions must eventually become as strong as hadron-hadron interactions. However, for the basic model of Ref. 2, the energies at which these strong effects begin to manifest themselves are unseasonably large -  $s > (10^{4} \text{ BeV})^{2}$  - and thus irrelevant for In Ref.2, we postulated a number of variants of the basic model which, SPEAR. though they are not as elegant as the basic model, do permit the lowering of this energy. Some of these models have other limitations - there is one, however, the prodigal model, which appears a "possible" candidate and which we further examine in this appendix in this regard. In summary, it appears that the severest restrictions on gauge models - if we wish to lower the energies at which electron-hadron interactions become effectively strong arise from the apparent absence of anomalous V-hadron couplings at low energies. This, in turn, leads to the conclusion that the electron must be strange - a conclusion consistent with the picture which appears to emerge from the phenomenological analysis of the text and which has strong implications for future experiments.

Α.

### The basic model and its problems

The basic model assigns the twelve quarks and the four (4-component) leptons to the Fermionic multiplets:

$$F_{L,R} = \begin{vmatrix} p_{a} & p_{b} & p_{c} & v \\ n_{a} & n_{b} & n_{c} & e^{-} \\ \lambda_{a} & \lambda_{b} & \lambda_{c} & \mu^{-} \\ \chi_{a} & \chi_{b} & \chi_{c} & v' \end{vmatrix}_{L,R}$$

(A.1)

with the symmetry group  $SU_L(4) \times SU_R(4) \times SU_{L+R}(4^{\circ})$ . For purposes of this appendix, the  $SU_L(4)$  and  $SU_R(4)$  groups, which after gauging of their  $SU_L(2) \times SU_R(2)$  subgroup, give rise to weak interactions - are basically irrelevant. The anomalous lepton-hadron interactions of concern to us in this paper arise from gauging the colour group  $SU(4^{\circ})$ . In the basic model, freedom from anomalies dictates that these interactions be purely <u>vector</u>. There are seven gauge-mesons which give rise to leptonic and semileptonic interactions; in the notation of the second paper of Ref.2, these are

-23-

 $s^{0}$ ; the exotics  $x^{0}$ ,  $x^{-}$ ,  $x^{-'}$ ; and the anti-exotics  $\overline{x^{0}}$ ,  $x^{+}$ ,  $x^{+'}$ 

The relevant interactions are:

$$\frac{f}{(24)^{\frac{1}{2}}} s^{0} \left[ \sum_{abc} (\overline{p}_{a} p_{a} + \overline{n}_{a} n_{a} + \overline{\lambda}_{a} \lambda_{a} + \overline{\chi}_{a} \chi_{a}) - 3(\overline{\nu}\nu + \overline{ee} + \overline{\mu}\mu + \overline{\nu}^{\dagger}\nu^{\dagger}) \right]$$

+ the exotic interactions:

$$f X^{0}(\overline{\nu p}_{a} + \overline{en}_{a} + \overline{\mu}\lambda_{a} + \overline{\nu'}\chi_{a})$$

$$+ f X^{-}(\overline{\nu p}_{b} + \overline{en}_{b} + \overline{\mu}\lambda_{b} + \overline{\nu'}\chi_{b}) \qquad (A.2)$$

$$+ f X^{-'}(\overline{\nu p}_{c} + \overline{en}_{c} + \overline{\mu}\lambda_{c} + \overline{\nu'}\chi_{c}) \quad .$$

The lower limits on the masses of  $S^0$  and the X-particles are given by the following relations:

1) The effective S<sup>0</sup>-coupling of v-hadronic interactions is 
$$\frac{f^2}{(m_S)^2}$$
 at  
low energy. Since this must be much smaller than  $G_F$  (in order that there  
are no unconventional weak-interaction effects at low energies), we conclude  
that:  
 $(m_S)^2 > G_F^{-1} f^2$ .

With  $\frac{r^2}{4\pi} \sim 1$ , this implies  $m_S \gtrsim 1000$  BeV.

The X-particles induce:

2)

$$\alpha^{0} \rightarrow \overline{\lambda} + n \rightarrow \mu^{-} + (\overline{X} + X) + e^{+} \rightarrow \mu^{-} + e^{+} ,$$

with the effective strength  $\approx \frac{f^2}{m_{\chi}^2}$ . Since  $K_L \Rightarrow \mu^+ + \mu^-$  amplitude  $\approx$   $G_F \alpha^2$ , and no events of the variety  $K_L \Rightarrow \mu^+ + e^\pm$  have yet been observed, we must have  $\frac{f^2}{m_{\chi}^2} \ll G_F \alpha^{-2}$ , i.e.  $m_{\chi}^2 \gg G_F^{-1} \alpha^{-2}$ ,  $(m_{\chi} > 3 \times 10^4 \text{ BeV})$ , for  $f^2/4\pi \sim 1$ .

To summarize, if we assume that  $f^2/4\pi \sim 1$ , the X's in the basic model must be superheavy (> 3 x 10<sup>4</sup> BeV) in order to suppress the  $K_L \rightarrow e+\mu$ transition. The X-mediated anomalous lepton-hadron interactions would then become effective only for energies in excess of 10<sup>4</sup> BeV and the model, as it stands,would be irrelevant to SLAC energies so far as its purely gauge interactions <sup>37)</sup> are concerned. If the model could be modified so that  $K \rightarrow e+\mu$  is rigorously forbidden, the severe limitation

-24-

on X-mass might be relaxed. Stated quantitatively, the  $e^{-e^+}$ annihilation data requires  $\epsilon \sim 1/50$  (see text). With  $(f^2/4\pi) (1/m_{\chi}^2) \simeq \epsilon \alpha/(BeV)^2$ , this implies a mass  $m_{\chi} \sim 100$  BeV (<u>heavy-X-case</u>) if  $f^2/4\pi \approx 1$ . If, on the other hand  $f^2/4\pi$  is of the order 38,39) 1/100 to 1/10, we need  $m_{\chi}$  to be as low as 10 to 30 BeV (<u>light-X-case</u>). In the next section we study how to forbid  $K \neq e + \mu$  and thus bring the X-mass down from being "superheavy" to just "heavy" or even "light".

One independent remark: In view of the fact that the rates of  $K_L \rightarrow \mu$ e-decays set the scale of energy at which the new class of interactions mediated by the X-particles become important in the basic model, we <u>especially</u> wish to urge a search for this decay mode. (Could it in fact be true that the rates of these decays are much larger than what are thought to be the upper limits for these decays?)

### B. <u>The prodigal model</u>

To forbid the  $K \neq e + \mu$  transition, we must make a distinction between the muon and the electron "colours"  $L_{\mu}$  and  $L_{e}$ . In the prodigal model we assume that the muon is, as it were, the news-bearer of the existence of a new heavier Fermionic multiplet with "new" quarks and new muonic leptons  $M^{O}$  and  $M^{-}$ . Thus we work with two basic multiplets:

•	p <sub>a</sub> p <sub>b</sub> p <sub>c</sub> E <sup>0</sup>		pi pi pi M <sup>O</sup>	
-	n n n E		n' n' n' M" a b c	(A.3)
e =	$\lambda_a$ $\lambda_b$ $\lambda_c$ e	• <sup>r</sup> u <sup>=</sup>	$\lambda_{a}^{i} \lambda_{b}^{i} \lambda_{c}^{i} \mu^{-}$	
	x <sub>a</sub> x <sub>b</sub> x <sub>c</sub> ν	L,R	ָּג' ג' ג' ג' ע'	L,R

Here  $E^0$ ,  $E^-$  and  $M^0$ ,  $M^-$  are heavy leptons with  $L_e = 1$  and  $L_{\mu} = 1$ , respectively, while the primed particles are new quarks. We assume that the

-25-

normal hadrons are made up of quarks in  $F_e$  (see remarks later). The ratio of masses of primed and unprimed quarks (and  $M^Q$  to  $E^Q$  leptons) may be  $\approx \frac{m_{\mu}}{m_e} \approx \alpha^{-1}$  (possibly as a consequence of a "natural"-symmetry-breaking mechanism where the masses for the  $F_e$  multiplet arise from "radiative" corrections of order  $\alpha$  to the masses of the  $F_u$  multiplet).

In order to gauge, we consider the local symmetries

$$SU_{L}(2) \times SU_{R}(2) \times SU_{e}(4') \times SU_{\mu}(4')$$

and the following interaction<sup>41)</sup>

$$g_{L}(\overline{F}_{eL} W_{L} F_{eL} + \overline{F}_{\mu L} W_{L} F_{\mu L}) + (L \rightarrow R) + f_{1} V_{1} (\overline{F}_{e} F_{e}) + f_{2} V_{2} (\overline{F}_{\mu} F_{\mu}) .$$
(A.4)

Both  $V_1$  and  $V_2$  are distinct vector particles corresponding to the colour gauge groups  $SU_e^{(4')}$  and  $SU_{\mu}^{(4')}$  respectively. The lighter e-type quarks and the very massive  $\mu$ -type quarks have no mutual interaction, except the weak and the electromagnetic, thus guaranteeing that normal hadrons may be considered as made up of e-type quarks only. (If one wished to minimize the mixing of  $V_1$  and  $V_2$  in the Lagrangian after spontaneous symmetry breaking, one simple assumption is to take all quarks  $q_e$ and  $q_{\mu}$  to be fractionally charged.<sup>42</sup> Another amusing possibility is that e-type quarks are integer and  $\mu$ -type quarks fractionally charged. In either case it is only the singlet fields  $S_1^0$  and  $S_2^0$  contained in  $V_1$  and  $V_2$ which need to be mixed to generate the massless photon through the Higgs mechanism.)

With this preparation and writing  $X_1$  and  $X_2$  interactions for  $F_e$  and  $F_{\mu}$  analogous to (A.2), one can now easily see that: 1) The model forbids  $K^0 \rightarrow e^- + \mu^+$ ; in fact all neutral decays provided  $m_{\overline{\mu}} > m_{\overline{K}}$ .

2) Since  $v_e$  is charmed and normal hadrons are not, the X-mechanism does not affect neutrino interactions  $v + H \rightarrow v + H$ . The S<sup>0</sup>-particles also do not lead to any anomalous enhancement of the neutrino interactions assuming that they are sufficiently massive.<sup>44</sup>

-26-

3) To forbid the enhancement of  $K^{+} \Rightarrow e^{+} + \overline{\nu}_{e}$  through X-mediation, the Cabibbo rotations must be made for the  $(n,\lambda)$  quarks with leptons (e,E)(and possibly also  $(\mu,M)$  and  $(n',\lambda')$ ) rotated in the same manner.<sup>45</sup> The  $\nu$ conventional rotation of leptons has important (though not easily measurable) consequences for the sequence of weak interaction constants. The weak Lagrangian now reads:

 $W_{L}\left[\overline{p}(n \cos\theta + \lambda \sin\theta) + \overline{\nu}_{e}(e \cos\theta + E \sin\theta) + \overline{\nu}_{\mu}(\mu \cos\theta + M \sin\theta)\right]$ 

Thus  $\beta$  decay versus  $\mu$  decay constants have the ratio 1:1 rather than  $\cos\theta$ :1, though K-decay versus  $\pi\text{-decay}$  constants still exhibit the ratio tan0.

4) The charmed character of  $\nu_e$  implies that its doublet-partner for  $SU_L(2)$ , i.e. the electron, is strange. With  $X_L$  mass arranged (through the Higgs mechanism) to be around 100 BeV, we obtain the desired enhancement of  $e^+ + e^- \rightarrow$  hadrons at SPEAR energies, though no anomalous  $\mu^+ + \mu^- \rightarrow$  hadron interaction is expected on account of the muon <u>not</u> being colour-coupled to normal hadrons which are assumed to be e-type quark composites. (For the model where e-type quarks are integer and  $\mu$ -type quarks are fractionally charged or vice versa, normal hadrons could contain contributions from <u>both</u> quark types and  $\mu^+ + \mu^- \rightarrow$  hadrons could also be anomalous.)

5) The "strange" character of the electron implies that  $\phi$ 's,  $\eta$ <sup>U</sup>'s would be predominantly produced as the SLAC energy goes up. In protonanti-proton annihilation there will be no anomalous production of  $e^+ + e^-$  pairs in the kinematic region where  $\lambda + \overline{\lambda}$  quark amplitude is not significant. Likewise, for a strange electron, the ratio  $\frac{e^+ + p + e^+ + H}{e^- + p^+ e^- + H}$  would not be affected appreciably by the X-mechanism.

To conclude, for the prodigal model (with new heavy leptons, with a "strange" electron and with two various types of quarks) the exotic gauge particle mediation can manifest itself as enhancing  $e^+ + e^- \rightarrow$  hadrons at SPEAR energies. Even though this model provides a natural "niche" for the muon, the fact that we had to double the number of Fermions makes the model somewhat unattractive. We ourselves prefer the basic model where X-particles are more massive than  $10^4$  BeV (if  $f^2/4\pi \sim 1$ ) and electron non-strange. But then who can dictate to Nature?

-27-

#### APPENDIX II

A general electron-lepton 4-Fermion interaction, relevant to our discussions in the text, is given by:

$$\begin{aligned} \mathcal{L} = \sum_{i} \left[ g_{S}^{i}(\overline{ee})(\overline{q}_{i}q_{i}) + g_{P}^{i}(\overline{e\gamma}_{5}e)(\overline{q}_{i}\gamma_{5}q_{i}) + g_{A}^{i}(\overline{ei\gamma}_{\mu}\gamma_{5}e)(\overline{q}_{i}i\gamma_{\mu}\gamma_{5}q_{i}) + g_{V}^{i}(\overline{e\gamma}_{\mu}e)(\overline{q}_{i}\gamma_{\mu}q_{i}) + g_{A}^{i}(\overline{ei\gamma}_{\mu}\gamma_{5}e)(\overline{q}_{i}i\gamma_{\mu}\gamma_{5}q_{i}) + g_{VA}^{i}(\overline{ei\gamma}_{\mu}\gamma_{5}e)(\overline{q}_{i}\gamma_{\mu}q) + g_{AV}^{i}(\overline{ei\gamma}_{\mu}\gamma_{5}e)(\overline{q}_{i}\gamma_{\mu}q) \right]. \end{aligned}$$

$$(A.5)$$

For the cases (IA, IB and II) discussed in Sec.III.1, the values of the coupling constants introduced above are as follows.[We give below <u>only those constants which are non-vanishing</u> for the case of electron being coupled to the n-quark (non-strange electron). The constants for the strange electron case are obtained by the substitution  $n \rightarrow \lambda$ .]

Case (IA) ("Vector-X"; (2(VV+AA) - (SS+PP))-effective interaction)

$$g_{V/4\pi\alpha}^{n} = g_{A/4\pi\alpha}^{n} = \epsilon/2$$

$$g_{S/4\pi\alpha}^{n} = g_{P/4\pi\alpha}^{n} = -\epsilon$$
(A.6)

where  $\varepsilon$  is defined by Eq.(4).

Case (IB) ((VV+AA)-effective interaction)

$$g_{V/4\pi\alpha}^{n} = g_{A/4\pi\alpha}^{n} = \varepsilon$$
 (A.7)

Case (II) ((V±A)(V±A)-effective interaction)

$$g_{V/4\pi\alpha}^{n} = g_{A/4\pi\alpha}^{n} = \varepsilon$$

$$g_{VA/4\pi\alpha}^{n} = g_{AV/4\pi\alpha}^{n} = \mp \varepsilon$$
(A.8)

If s is in the asymptotic region (so that parton-model considerations may be applied) but <u>not</u> high enough to invalidate the local 4-Fermion interaction approximation given by Eq.(A.5), the cross-section for  $e^-e^+ \rightarrow$  hadrons is given for the <u>HEAVY-X-CASE</u> by:

-28-

$$\begin{split} \sigma(e^+e^- + \mathrm{hadrons}) &= \frac{4\pi\alpha^2}{3s} \left[ \sum_{i} Q_i^2 \right] + \frac{s}{16\pi} \left[ \sum_{i} \left\{ (g_S^i)^2 + (g_P^i)^2 \right\} \right] \\ &+ \frac{s}{12\pi} \sum_{i} \left[ (g_V^i)^2 + (g_A^i)^2 + (g_{VA}^i)^2 + (g_{AV}^i)^2 \right] \\ &+ \frac{2}{3} \alpha \left[ \sum_{i} Q_i g_j^V \right] \quad , \end{split}$$

where |e|Q, denotes the charge of the ith quark and s is centre of mass  $(energy)^2$ .  $e^{\frac{t}{p}} \rightarrow e^{\frac{t}{t}} + H$ 

The ratio of  $(e^+p)$  and  $(e^-p)$  cross-sections for given values of incident lepton energy E, scattering angle  $\theta$  and momentum transfer square  $q^2$ , is given by:

$$\frac{d\sigma^{e^{-}}(E,\theta,q^2)}{d\sigma^{e^{-}}(E,\theta,q^2)} = \frac{X_+}{X_-} , \qquad (A.10)$$

(A.9)

where, with the interaction (A.5) (and parton model hypothesis)  $X_{\pm}$  are given by  $\frac{47}{2}$ :

$$\begin{aligned} \kappa_{\pm} &= \sum_{i} \left[ f_{i}(\mathbf{x}) \quad \left[ \left[ \frac{Q_{i}}{q^{2}} + \frac{g_{V}^{i}}{e^{2}} \right]^{2} + \left[ \frac{g_{A}^{i}}{e^{2}} \right]^{2} + \left[ \frac{g_{VA}^{i}}{e^{2}} \right]^{2} + \left[ \frac{g_{AV}^{i}}{e^{2}} \right]^{2} \right] (1 - y + y^{2}/2) \\ &+ \left[ (g_{S/e^{2}}^{i})^{2} + (g_{P/e^{2}}^{i})^{2} \right] y^{2}/4 \\ &\pm \xi_{i} \left[ \left[ \frac{Q_{i}}{q^{2}} + \frac{g_{V}^{i}}{e^{2}} \right] \left[ \frac{g_{A}^{i}}{e^{2}} \right] + \frac{g_{VA}^{i}}{e^{4}} \right] y(2 - y) \right] , \end{aligned}$$
(A.11)

where  $x = 1/\omega = -(q^2/2M_N v)$ ,  $y = (p \cdot q/p \cdot k)$  and  $v = (p \cdot q)/M_N = E - E'$ . The quantities p and k denote the 4-momenta of the incoming nucleon and lepton, respectively, while q is the 4-momentum transfer between the incoming and outgoing leptons. The factor  $\xi_i$  is +1 for ith quark and -1 for ith anti-quark. The function  $f_i(x)$  denotes the ith type quark momentum distribution within the proton.

-29-

Structure functions

The general formulae for the functions  $vW_2$ ,  $MW_1$  and  $vW_3$  defined by Eq.(11) are given by:

$$vW_{2}(q^{2},v) = x \left[ \sum_{i} Q_{i}^{2} f_{i}(x) + q^{4} \sum_{i} \left\{ \left[ \frac{g_{V}^{i}}{e^{2}} \right]^{2} + \left[ \frac{g_{A}^{i}}{e^{2}} \right]^{2} + \left[ \frac{g_{AV}^{i}}{e^{2}} \right]^{2} + \left[ \frac{g_{AV}^{i}}{e^{2}} \right]^{2} \right\} f_{i}(x)$$
$$+ 2q^{2} \sum_{i} \left[ \frac{g_{V}^{i}}{e^{2}} \right] Q_{i} f_{i}(x)$$

-30-

$$M_{N}W_{1}(q^{2},v) = \frac{1}{2} \sum_{i} Q_{i}^{2} f_{i}(x) + \frac{q^{4}}{4} \sum_{i} \left\{ \left[ \frac{g_{S}^{i}}{e^{2}} \right]^{2} + \left( \frac{g_{P}^{i}}{e^{2}} \right]^{2} \right\} f_{i}(x)$$

$$vW_{3}(q^{2},v) = \pm \sum_{i} \left[ \left\{ Q_{i}q^{2} + \left( \frac{g_{V}^{i}}{e^{2}} \right) q^{4} \right\} \left[ \frac{g_{A}^{i}}{e^{2}} + \left( \frac{g_{V}^{i}}{e^{2}} \right) \left[ \frac{g_{AV}^{i}}{e^{2}} \right] \right] 2f_{i}(x)$$

(A.12)

where the  $\pm$  signs are for  $e^{\pm}p$ -scatterings.

#### REFERENCES AND FOOTNOTES

- J.C. Pati and Abdus Salam, Review lecture by Prof. J.D. Bjorken, Proceedings of the 16th International Conference on High Energy Physics (1972), Vol.2, p.304; Phys. Rev. D8, 1240 (1973).
- J.C. Pati and Abdus Salam, Phys. Rev. Letters <u>31</u>, 661 (1973);
   Phys. Rev. (1 July 1974).
- 3) B. Richter (Report of SPEAR data); Irvine Conference on Lepton-Induced Reactions, Irvine, California, December 1973; Rapporteur's talk at the 17th International Conference on High Energy Physics, London, July 1974.
- 4) J.C. Pati and Abdus Salam, Remark at the Irvine Conference, December 1973; Phys. Rev. Letters <u>32</u>, 1083 (1974).
- 5) See Rapporteur's talk by L. Lederman at the 17th International Conference on High Energy Physics, London, July 1974, for relevant experimental data on this point.
- 6) Preliminary SLAC data reported by E.D. Bloom at the Topical Meeting on the Physics of Colliding Beams, Trieste, Italy, 20-22 June 1974, and by R. Taylor at the 17th International Conference on High Energy Physics, London, July 1974. We thank Professor Bloom and Professor Taylor for discussions of this data.
- 7) L. Hand (private communication).
- 8) Quite possibly, all interactions (including strong) may start as chiral gauge interactions with (V-A) and (V+A) currents coupled to distinct massless gauge mesons  $X_L$  and  $X_R$  with equal coupling strengths  $f_L$  and  $f_R$ . Parity conservation would hold only provided spontaneous symmetry breaking arranges itself to lead to  $(X_L \pm X_R)/\sqrt{2}$  as the eigenstates of the gauge meson mass matrix. These, as well as alternative possibilities with  $X_L$  and  $X_R$  being eigenstates, may be realized in the context of the prodigal model discussed in Appx.I.
- 9) Some relevant tests have been suggested in a recent note by M.A.B. Bég and G. Feinberg, Rockefeller Univ. preprint, COO-2232 B-52, 1974.
- 10) For example, I.I.Y. Bigi and J.D. Bjorken in a recent paper (SLAC-PUB-1422, 1974) have made the assumption for a number of their considerations that all quarks are involved in anomalous lepton-hadron interactions with the same strength. This may appear difficult to arrange in a normalizable gauge theory and in any case it is not permissible in our scheme. Due to this difference, there are significant quantitative differences with regard to deviations from scaling with our without

-31-

scalar 4-Fermion interaction (see remarks later).

- 11) However, it should be remarked that as yet we have not been able to construct a model in which e is non-strange (as in (i)) and at the same time the anomalous X-interactions are relevant at SPEAR energies. The other two choices with e strange are realized in realistic models (see Appx. I).
- 12) In general, in this case, one may allow (V+A) as well as (V-A) interactions with different strengths.
- 13) A phenomenologically minded reader may have reservations on the precise values of these constants, dependent as they are on parton model considerations.
- 14) Since <u>only</u> the n or the  $\lambda$ -quark is coupled to  $e^-$  via X, one obtains the same result for  $q_e = n$  or  $\lambda$ . Note also that the result, in this case, is the same for the fractionally charged quark (i.e. electric charge -|e|/3 for all three colours) or the integer charge quark (i.e. electric charges (-1,0,0)|e| for the three colours (a,b,c)).
- 15) In models with integer charge quarks, the colour-octet of gluons carry electric charges (see Ref.l), which should also contribute to  $\rho_{\gamma\gamma}(s)$  above the "colour-thaw" threshold.
- 16) Formula (7) will need modification if new channels involving charm and/or colour open at some intermediate energy. This will modify the 1-photon contribution to  $\sigma_{\rm h}(s)$  leading to a threshold behaviour over a range of energy followed by an increase in  $\Sigma q_i^2$  sufficiently above the threshold.
- 17) A still higher value of  $\Sigma Q_1^2$  like 6 corresponding to three quartets of integer charge quarks with <u>both</u> colour and charm having been excited appears not to give a good fit to the  $e^-e^+$ -annihilation data at lower values of centre-of-mass of (energy)<sup>2</sup> like s = 7 to 10 (BeV)<sup>2</sup>.
- 18) These would include masses of Higgs-particles of the light variety (5 ~ 10 BeV), which do arise in our theory(see remarks later, Footnote 37). To study the energy dependence for the light-X-case, we have considered a simple example of an X-mediated box diagram for  $e^+ + e^- \rightarrow \sigma + \sigma$ , where  $\sigma$ 's are spin-zero objects, in the region  $m_X^2 \leq s \leq m_q^2$ , where  $m_q$  is quark mass, and find a dependence of the type  $\frac{4\pi}{3} \left[ \alpha^2 - \frac{\Sigma Q_1^2}{s} + \delta + \delta' \sqrt{s} \right]$ , i.e. less steeply rising than (7).

-32-

- 19) See, for example, J.D. Bjorken, "High transverse momentum processes", talk given at the 2nd Aix-en-Provence Conference, 1973.
- 20) If the muon is coupled to the  $\lambda$ -quark, the ratio of  $(\mu^{\dagger}N/\mu^{-}N)$  cross-sections is expected to remain unity for all  $q^2$  and  $\omega$  if  $f_{\lambda}(x) = f_{\overline{\lambda}}(x)$  within the nucleon for all x.
- 21) We should emphasise that there is no compelling reason (in the absence of an experiment of the type  $\mu^- + \mu^+ \rightarrow$  hadrons) to assume that the muon is involved in the anomalous interaction with the same strength as the electron.
- 22) The contribution of the  $vW_3$ -term may be eliminated by combining  $(e^+p)$  with  $(e^-p)$  data.
- 23) We thank C.H. Llewellyn Smith for emphasising this point to us.
- 24) This point has been independently noted by A. Soni, Columbia University preprint, CO-2271-38, 1974.
- 25) This was kindly pointed out to us by G. Feinberg (private communication) and has been stressed in a recent paper by M.A.B. Bég and G. Feinberg (Ref.9). As discussed in the text, the conclusion drawn in this paper appears to be overstated in the context of our models. This is because in our gauge models the electron is NEVER coupled to the proton - a restriction which Bég and Feinberg do not impose.
- 26) For a recent review see B. E. Lautrup, A. Peterman and E. de Rafael, Phys. Reports <u>3C</u>, 193 (1972) and review talk by N. Kroll, 3rd Int. Conf. on Atomic Physics, Boulder, Colorado (1972)-UCSD-10P10-110.
- 27) The possible significance of π<sup>0</sup> → e<sup>+</sup>e<sup>-</sup>-decay for our considerations has been emphasised to us by M. Gell-Mann and C.H. Llewellyn Smith and has been discussed in two recent papers (Ref. 24 and Ref. 28, see below). There appears to be an incorrect statement in Ref. 24 with regard to contributions from (V+A) and (S-P) covariants in the starting Yukawa interaction.
- 28) J.D. Davies, J.G. Guy and R.P.K. Zia, Rutherford Laboratory preprint R1-74-092, 1974; also C.H. Llewellyn Smith (private communications).
- 29)  $\eta \rightarrow e^+e^-$ -decay is discussed in Ref.10. See, however, remarks on the value of  $h_n$  in the text.

-33-

- 30) N. Barash-Schmidt, et al., Rev. Mod. Phys., 1 April 1974.
- 31) This has also been noted independently by H.S. Mani (private communications), A. Soni (Ref.24), and Bjorken and Bigi (Ref. 10).
- 32) See Ref.24 for evaluation of these coefficients in some specific cases.

33) J.H. Christenson <u>et al</u>., Phys. Rev. D<u>8</u>, 2016 (1973).

- 34) See, for example, remark by J.D. Bjorken at the 17th International Conference on High Energy Physics, London, July 1974.
- 35) We thank Professor L. Lederman for this remark.
- 36) This is, provided  $f^2$  is large (i.e.  $f^2/4\pi \sim 1$ ). See, however, remarks later.
- Of course, even in the basic model, it is possible that Higgs-scalars 37) may provide the desired anomalous lepton-hadron interactions. Some specific possibility of this kind (involving s-channel exchanges in  $e^{-}e^{+}$  + hadrons) has been suggested by T. Goldman and P. Vinciarelli, If experiments establish a predominantly SLAC-PUB-1407, 1974. scalar-pseudoscalar interaction (possibly through polarization measurement mentioned by these authors and in Ref.10), it is worth remarking that the pseudo-Goldstone particles of masses 5~10 BeV or their composites with each other or with the X's in our basic model could be the objects which are the relevant ones. Some of these particles would have the quantum numbers of X-particles. For a discussion of the pseudo-Goldstone particles in our basic model see D.A. Ross, Imperial College, London, preprint IC/73/19, 1974.
  - 38) Such a low effective coupling in the X-subsector together with (perhaps) a larger effective coupling in the SU(3')-sector (giving rise to low energy "strong" interactions) may well arise due to finite renormalization effects following spontaneous symmetry breaking.

As pointed out in a general context in Ref. 1, the <u>effective</u> coupling of X-mesons need not be identical to the coupling of the SU(3')-colour octet gauge mesons, even though these latter particles belong to the same 15-fold of SU(4') as the X's. This is because (finite) renormalization effects following spontaneous symmetry breaking is likely to affect these various particles differently. We plan to investigate this question in detail in a subsequent note. As regards the coupling in the SU(3')sector, a recent estimate, though crude, suggests that the effective

-34-

constant  $f^2(\mu)/4\pi$  renormalized at the mass  $\mu = 2$  BeV may be as small as 1/10 (H.D. Politzer, to be published). These estimates apply to our scheme.

- 39) All effective constants may approach the value ≈ 1/137 at sufficiently high energies in a theory with universality of coupling constants, is an idea suggested recently by a number of authors in the interest of complete unification of all interactions, see, for example, H. Georgi and S.L. Glashow, Phys. Rev. Letters <u>32</u>, 438 (1974); H. Fritsz and P. Minkowski, CALTECH, preprint, 1974. Our scheme may be imbedded in a bigger group (like SU(16)) to achieve universality of coupling constants.
- 40) Note that the heavy lepton search based on  $\nu_{\mu}$ -induced reactions (see for example, B.C. Barish <u>et al.</u>, Phys. Rev. Letters <u>32</u>, 1387 (1974)) applies to the heavy lepton M<sup>-</sup> introduced here only to the extent of the Cabibbo rotation ( $\theta_{\mu}$ ) in the (n', $\lambda$ ') and ( $\mu$ ,M) spaces. The amplitude for  $\nu_{\mu} \neq M^{-} + W^{+}$  is proportional to sin $\theta_{\mu}$  (see remarks later).
- 41) A second anomaly-free interaction could be written down with the form:

 $f V_1 (\overline{F}_{eL} F_{eL} + \overline{F}_{\mu R} F_{\mu R}) + f V_2 (\overline{F}_{\mu L} F_{\mu L} + \overline{F}_{eR} F_{eR})$ 

Here, spontaneous symmetry-breaking must be arranged to guarantee that it is  $(V_1 + V_2)$  and  $(V_1 - V_2)$ , which are the physical particles and are vector and axial-vector, respectively. [Strictly speaking, one needs to arrange that parity is conserved at least in the  $SU(3^{\dagger})$ sector, i.e.  $(V_1(\underline{\beta}) \pm V_2(\underline{\beta}))$  are the physical particles, leaving the the possibility that in the X-sector the interactions are still chiral and parity violating with  $X_1$  and  $X_2$  being the eigenstates. We do not exhibit this here but have verified that such patterns of mixing are obtainable through Higgs-Kibble mechanism.] One distinct advantage of this version is that it is  $\gamma_5\text{-invariant}$  in the X-sector (in contrast to our basic model or the prodigal model (Eq.(A.4))). This may help preserve the masslessness of 4-component neutrino ( $v_e$  and  $v_u$ ) without a necessity for introducing the Z-Fermions (see the second paper of Furthermore (due to  $\gamma_5$ -invariance), it also depresses Ref.2, Sec.5.2). contributions to the anomalous magnetic moments of e and  $\mu$  from lighter mass X-exchanges. (See remark in Ref.4, Footnote 8). This fact is reflected in Table IV. In this version, the two types of quarks (both necessarily integer or fractionally charged for parity conservation) mutually interact through (at least)  $(V_1(8) + V_2(8))$ 

-35-

and  $(V_1(\underline{\aleph}) - V_2(\underline{\aleph}))$  fields. Normal hadrons may still be assumed to be predominantly e-quark composites with  $\mu$ -quark composites lying higher due to the heavier mass of the  $\mu$ -quarks. Small admixtures of  $(\overline{\lambda}'\lambda')$  with  $(\overline{\lambda}\lambda)$  (for example) are of course harmless.

- 42) If both types of quarks  $q_e$  and  $q_{\mu}$  are integer charged, the charge formula receives symmetric contributions from SU(4), SU(4')<sub>e</sub> and SU(4')<sub>µ</sub> generators. The SU(3') octet of gluons  $V_e(8)$  must mix with  $V_{\mu}(8)$  to generate the photon. Remarks made earlier (see end of previous footnote) with regard to composition of normal low-lying hadrons would apply here as well.
- 43) Once again, we have verified that such a mixing can be realized through the Higgs-Kibble mechanism. The scalar multiplets necessary for this purpose and their potential are simple generalizations of those presented in Ref.2 for the case of the prodigal model with two different SU(4') groups. These may be presented in detail elsewhere.
- 44) Note that the mass of the singlet  $S^0$  can be made as large as desired compared with the masses of the exotics  $m_X$  by introducing reducible Higgs multiplets of the type (1,1,4 x 4 x 4, 1) to generate  $V_1$ masses and (1,1,1,4 x 4 x 4) to generate  $V_2$  masses. This could then ensure the possibility that neutrino interactions mediated by  $S^0$  are not unduly enhanced at present energies, while electron (and possibly muon) interactions with hadrons mediated by X's are enhanced to the extent observed at SPEAR. As noted in Ref.2 (second paper), Sec.4.5, large reducible multiplets such as mentioned above are also needed, if one desires to give masses to the SU(3') colour octet of gluons in a model with fractionally charged quarks.
- 45) Of course, in general, one may also allow Cabibbo rotations for  $F_e$ and  $F_{\mu}$  to be <u>different</u>, which will lead to the coupling:  $W_L[\bar{p}(n \cos\theta_e + \lambda \sin\theta_e) + \bar{\nu}_e(e \cos\theta_e + E \sin\theta_e) + \bar{\nu}_{\mu}(\mu \cos\theta_{\mu} + M \sin\theta_{\mu})]$ . This will lead to  $\mu$  decay versus  $\beta$  decay constants to have the ratio  $\cos\theta_{\mu}: \cos\theta_{e}$ , while  $K \neq e\nu$  versus  $\pi \neq e\nu$  constants to have the ratio  $\tan\theta_e$ , etc. Note that such rotation of leptons (with e and  $\mu$  belonging to <u>different</u> colours) do not affect the rate of  $\mu \neq e + \gamma$ decay and the 2-neutrino experiment.

-36-

46) Noting that  $\eta^0$  primarily decays through neutral modes, this may provide an ingredient to explain the so-called energy crisis. See, for example, C.H. Llewellyn Smith, CERN preprint TH.1849, 1974. Note (since  $(\overline{\lambda}\lambda)$ ) density relevant to the case of the strange electron is isoscalar), the physical  $\phi$  and  $\eta^0$  production in  $e^{-e^+} \rightarrow$  hadrons at higher energies must be accompanied by at least 2-pion production or other multiparticle states to balance I-spin and energy-momentum conservation.

-37--

47) This formula, in this generality, is due to C.H. Llewellyn Smith.

· ·	IA ('	IA ("vector"-X)		IB((VV + AA)-Eff.Int.)		II ((V±A)(V±A)·Eff. Int)	
	q <sub>e</sub> = n	$q_e = \lambda$	q = n	$q_e = \lambda$	$q_e = n$	$q_e = \lambda$	
$\frac{e^+ p}{2-p}$ (q <sup>2</sup> = -15							
$E = 13.9 \ \theta = 50^{\circ}$ )	1.18	1.0	1.43	1:0	1.63	1.0	
"Violation of Scaling" $(q^2 = -25, \omega = 1.5)$		· · ·				· · · · · · · · · · · · · · · · · · ·	
In MW	14%	< 5%	0	0	0	0	
$\ln v W_2$	13%	< 5%	50%	< 5%	80%	< 5%	
HFS-Splitting (Parts per million)	-2	≈ 0	-4	. ≃ 0	4	≃ 0	
$\pi^{\circ} \rightarrow e^{+}e^{-}$ (Branching Ratio)	$(h_{\pi}/m_{\pi})^{2}(5\times10^{-4})$	) ≃ 0	$2.5 \times 10^{-8}$	≃ 0	2.5x10 <sup>-8</sup>	≃ 0	
Anomalous mag. mom. of e and $\mu$	Need M <sub>q</sub> 1	to be small <sup>††</sup>	sup	pressed <sup>41)</sup>	suppr	41) ressed	

TABLE IV

<sup>††</sup>See Footnote 8 (Ref. 4)